

Comparing Analysis Strategies

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UC San Diego

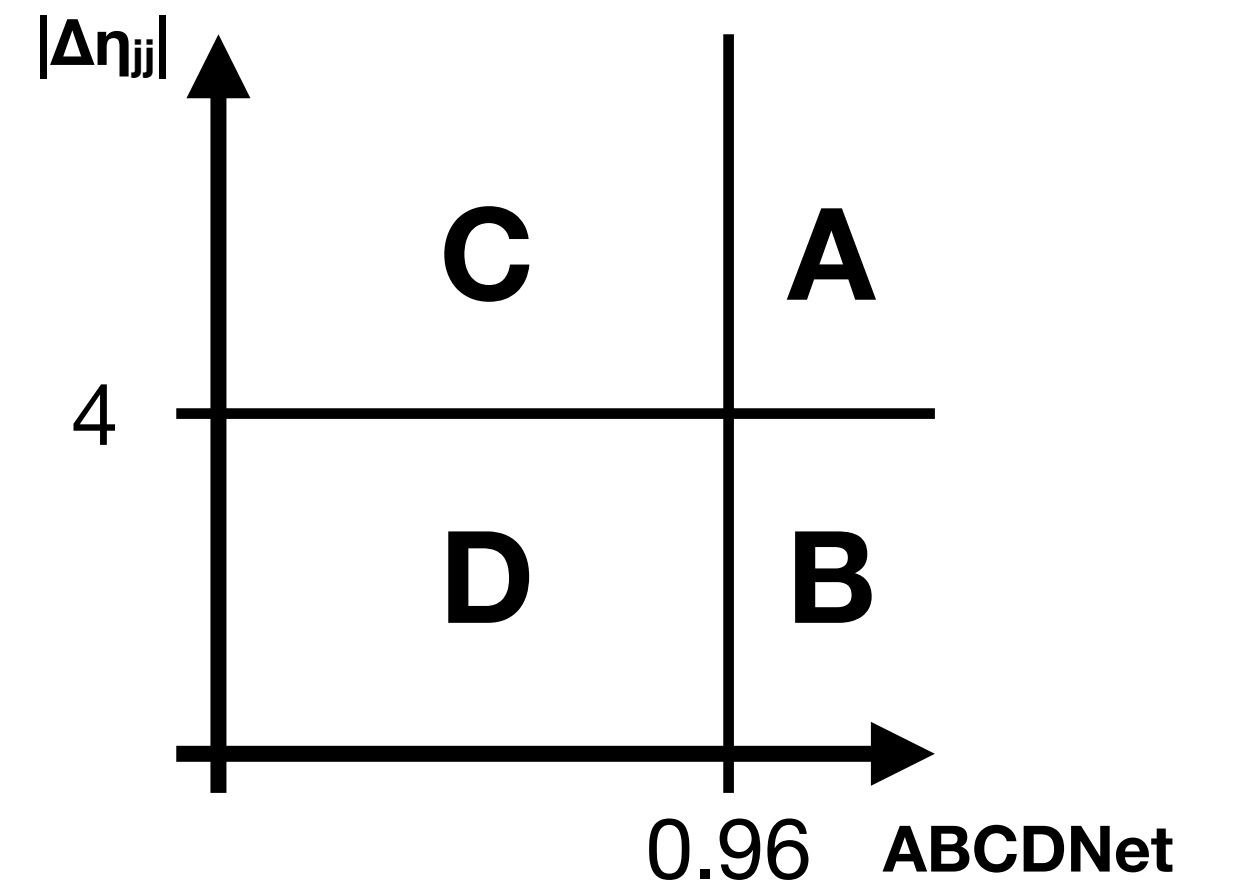
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Overview

- ABCD shown to L3s (right) had limited statistics in Region B
- This resulted in a systematic uncertainty of $\sim 50\%$
- Trying two more strategies:
 - ABCDNet vs. VBS BDT
 - ABCDNet vs. VBS DNN
- Then we compare: **is there a clear best strategy?**

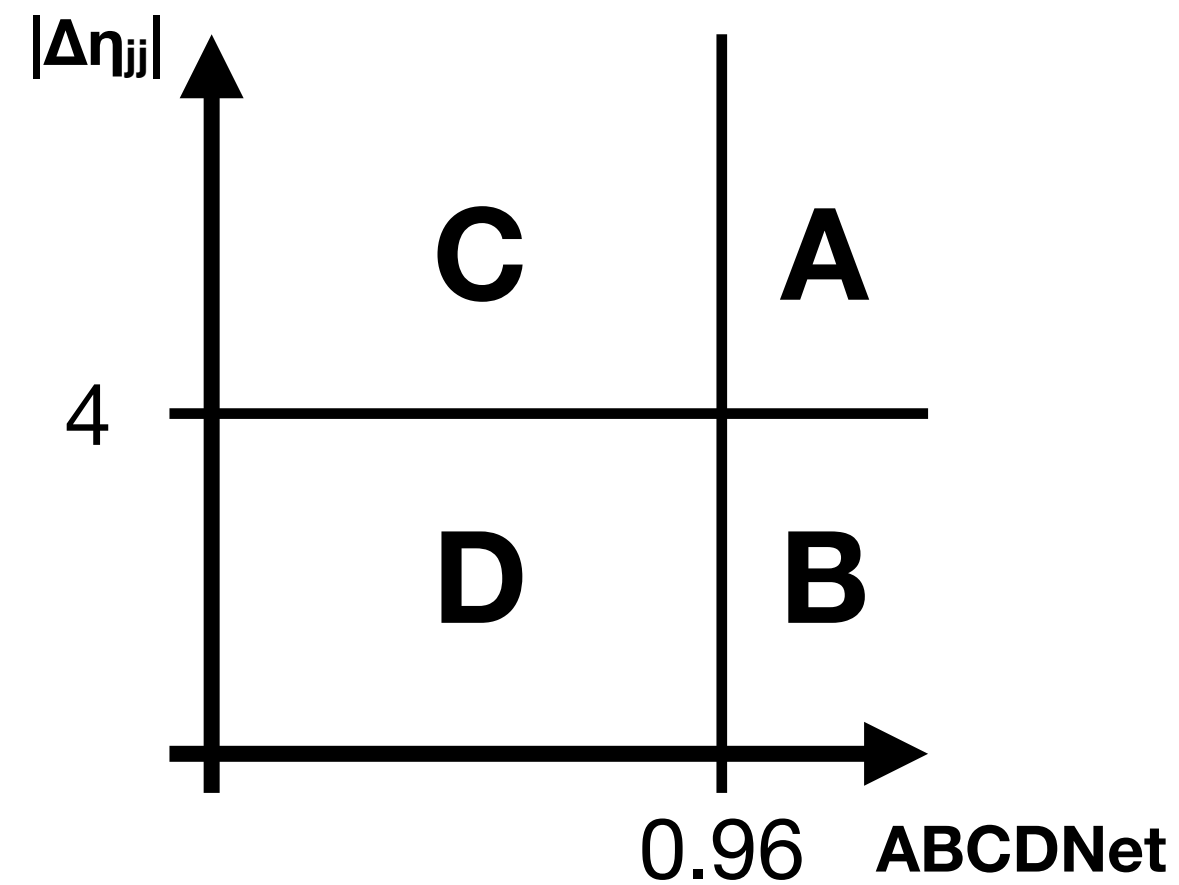
$X_{bb} > 0.6$ and $X_{Wqq} > 0.75|0.7$ ($l_d|tr$)



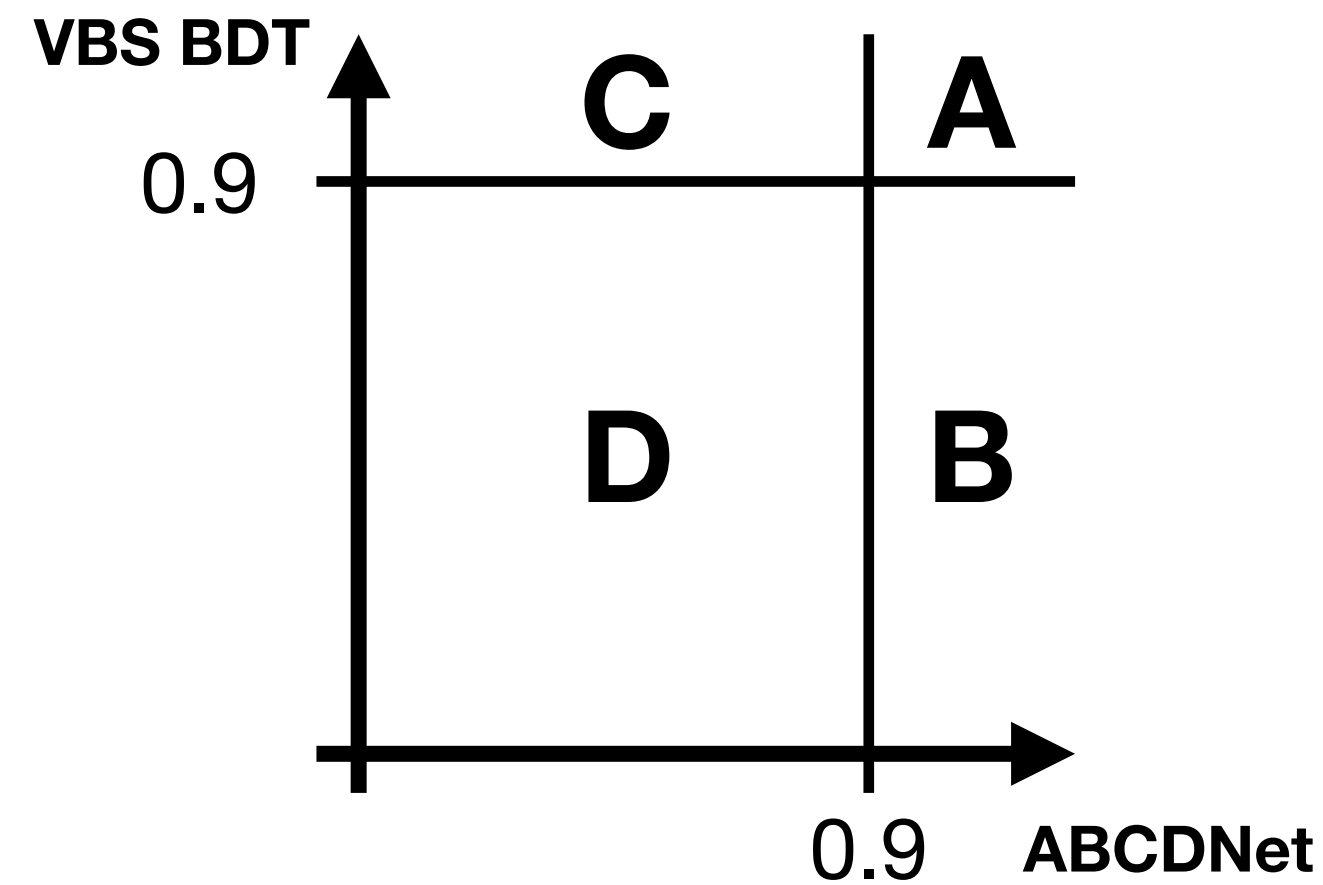


Comparison

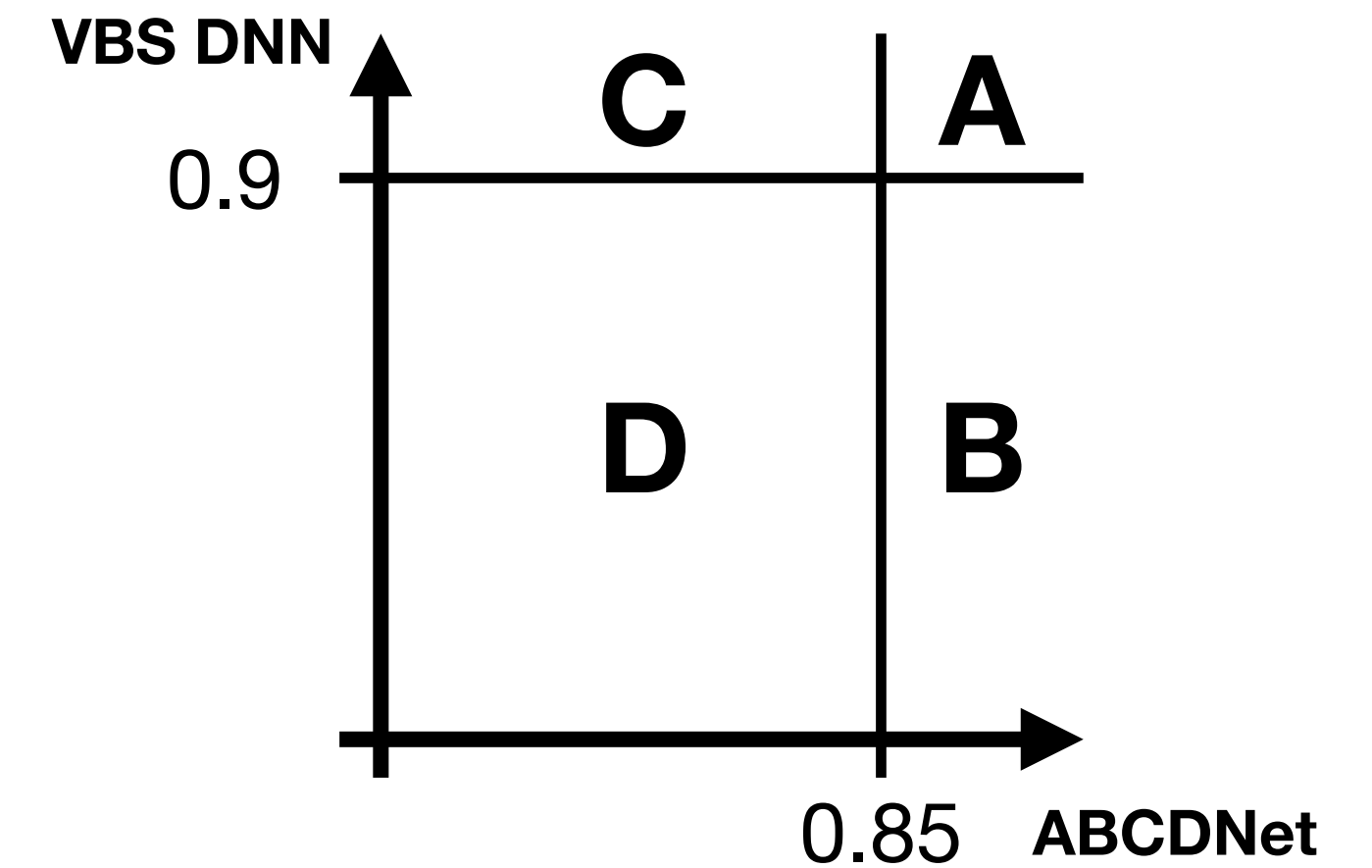
$X_{bb} > 0.6$ and $X_{Wqq} > 0.75|0.7$ (ld|tr)



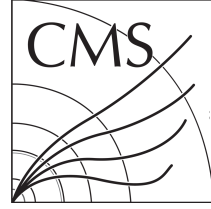
$X_{bb} > 0.8$ and $X_{Wqq} > 0.6|0.4$ (ld|tr)



$X_{bb} > 0.5$ and $X_{Wqq} > 0.5|0.4$ (ld|tr)

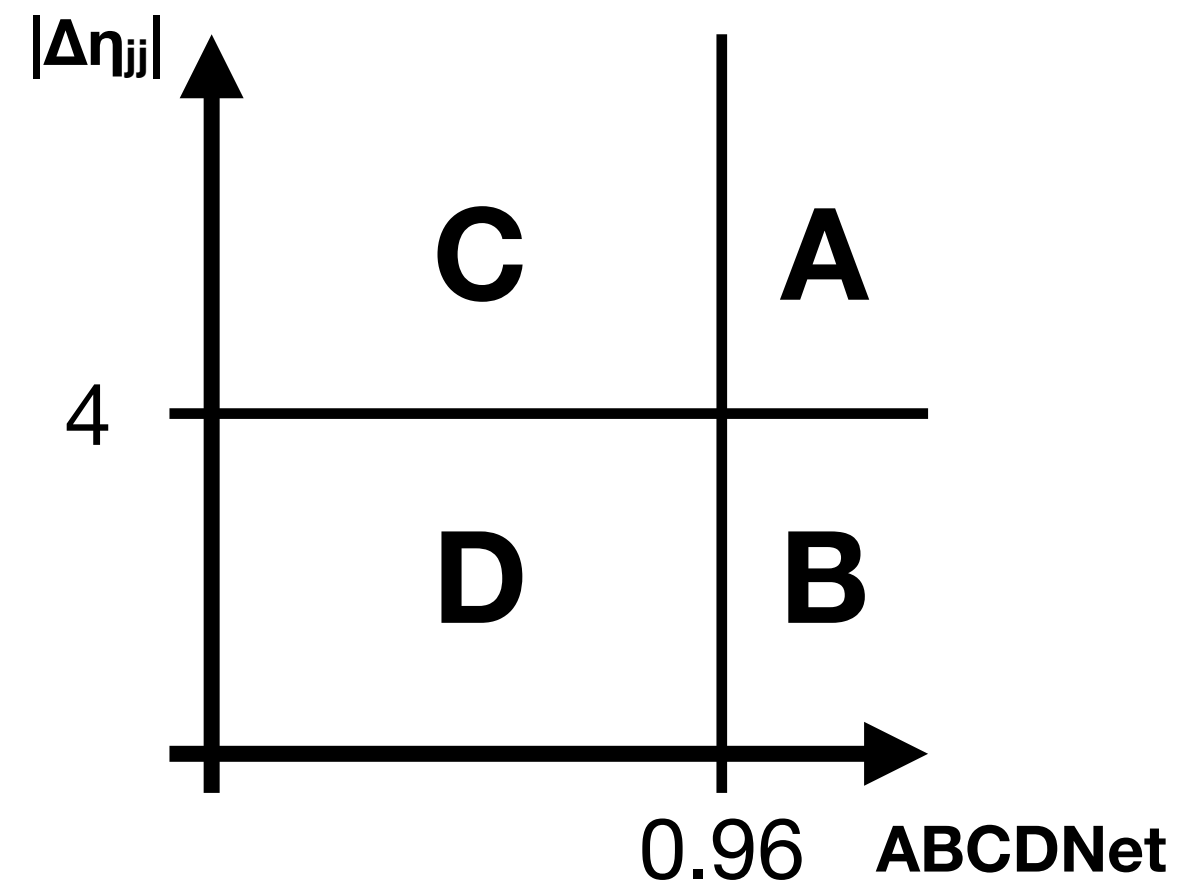


	ABCDNet vs. $ \Delta\eta_{jj} $	ABCDNet vs. VBS BDT	ABCDNet vs. VBS DNN
Signal	3.73	3.80	6.88
Predicted Bkg.	0.93	1.09	0.78
ABCD Stat. Unc.	50.4%	18.9%	18.9%
ABCD Syst. Unc.	29.5%	62.9%	32.9%
Data/MC	OK	OK	Some issue from D→C
Closure in data	Good	Good, but limited by signal contamination	Good

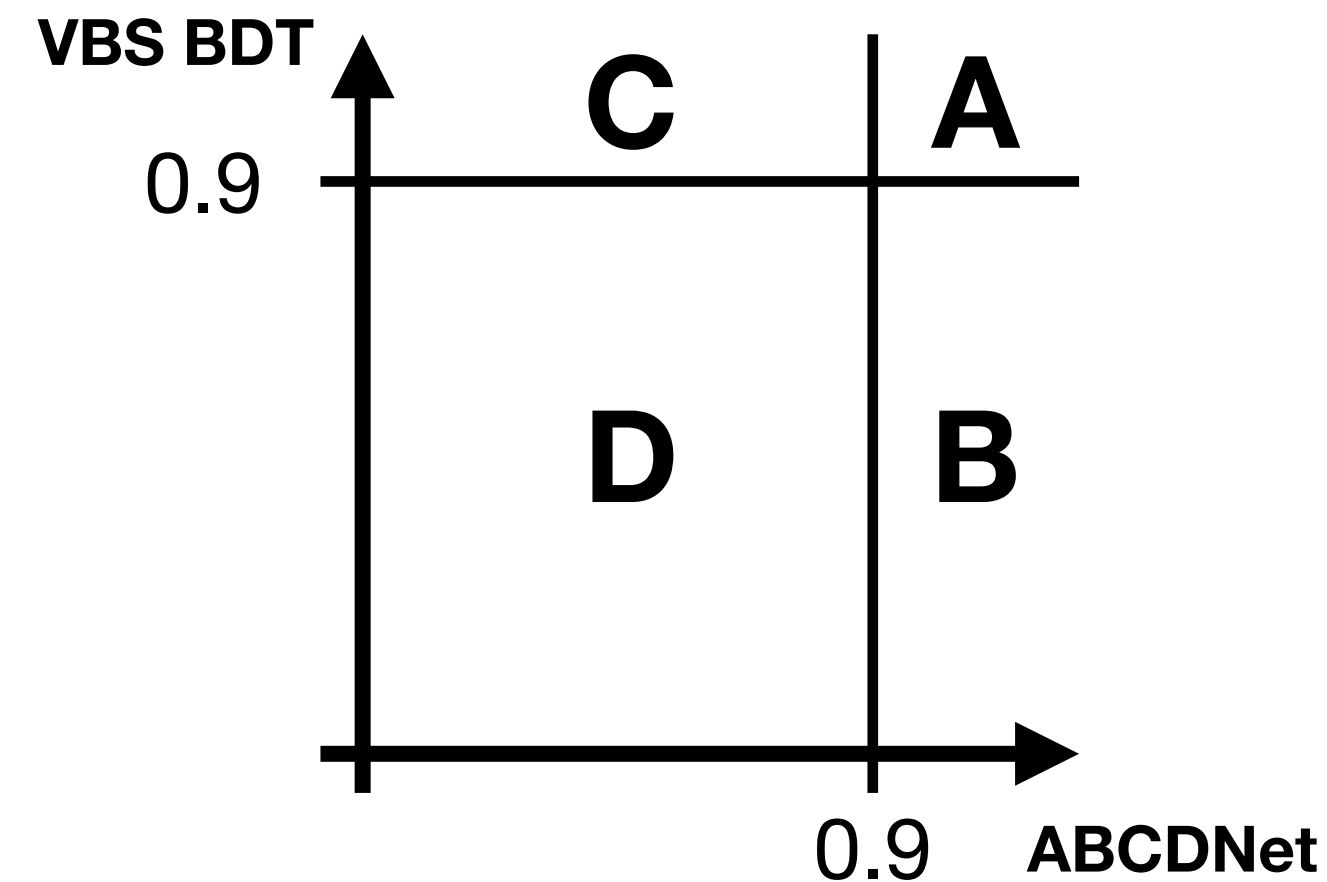


Summary

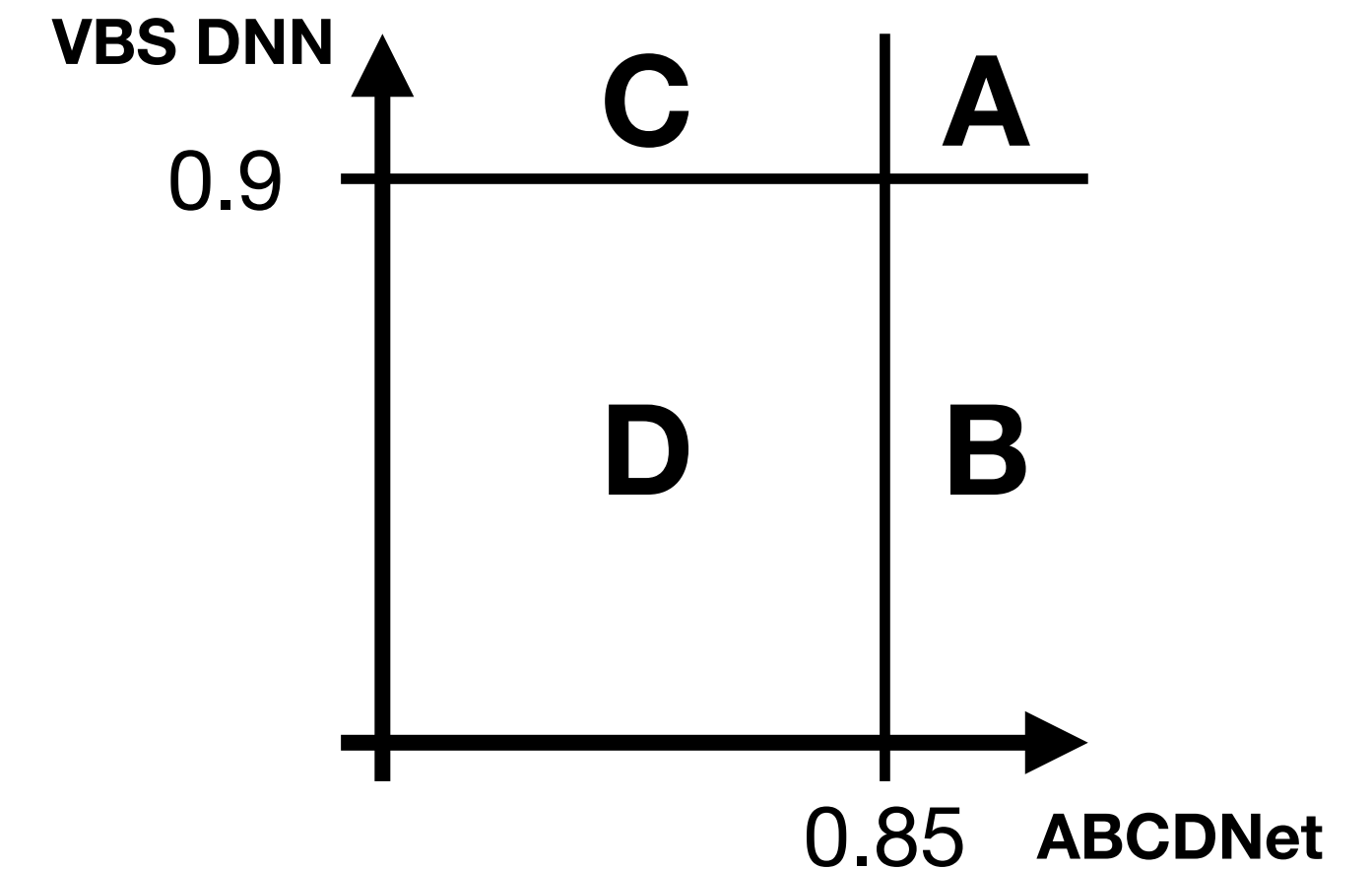
$X_{bb} > 0.6$ and $X_{Wqq} > 0.75|0.7$ (ld|tr)



$X_{bb} > 0.8$ and $X_{Wqq} > 0.6|0.4$ (ld|tr)

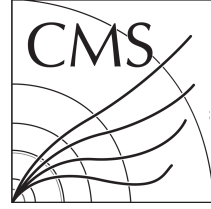


$X_{bb} > 0.5$ and $X_{Wqq} > 0.5|0.4$ (ld|tr)

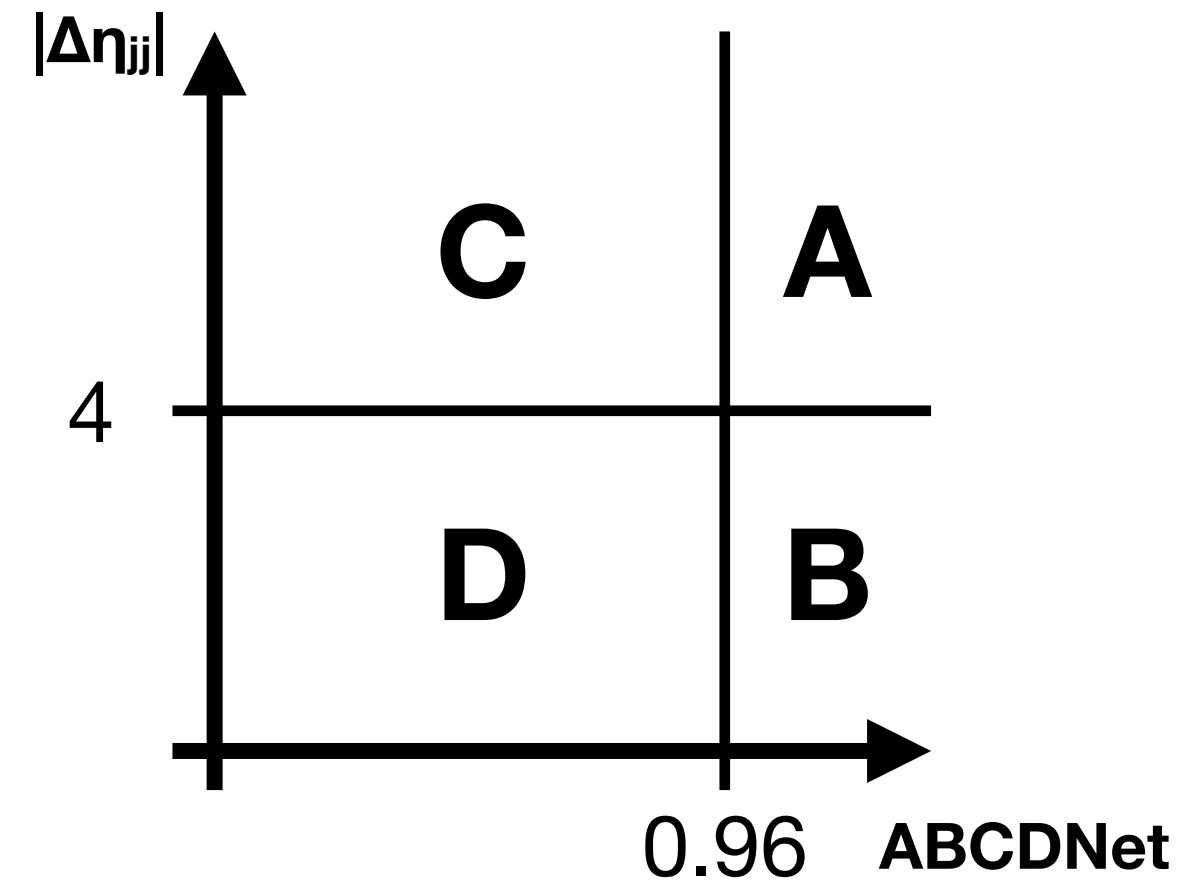


- No one “best” method
- Systematic uncertainty may need rethinking (seems unfair?)
- VBS BDT method is nice, but sig. contamination limits data closure tests
- VBS DNN method is tempting... but do we believe it?

ABCD: ABCDNet vs. $|\Delta\eta_{jj}|$ (orig.)



ABCD Configuration & MC Closure



$X_{bb} > 0.60$ and $X_{Wqq} > 0.75|0.70$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
$ \Delta\eta_{jj} > 4$ and $ABCDNet > 0.96$	A	1.46	0.54	3.73	0.05	—	—
$ \Delta\eta_{jj} \leq 4$ and $ABCDNet > 0.96$	B	5.12	1.06	0.48	0.02	4	2.00
$ \Delta\eta_{jj} > 4$ and $ABCDNet \leq 0.96$	C	292.88	25.89	2.80	0.05	280	16.73
$ \Delta\eta_{jj} \leq 4$ and $ABCDNet \leq 0.96$	D	1012.41	41.07	0.63	0.02	1201	34.66

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{1.48 \pm 0.34}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{0.93 \pm 0.47}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{1.47}} \sqrt{\left(\frac{\mathbf{0.54}}{\mathbf{1.46}}\right)^2 + \left(\frac{\mathbf{0.34}}{\mathbf{1.48}}\right)^2} = 29.5\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 50.4\%$$

Final Result

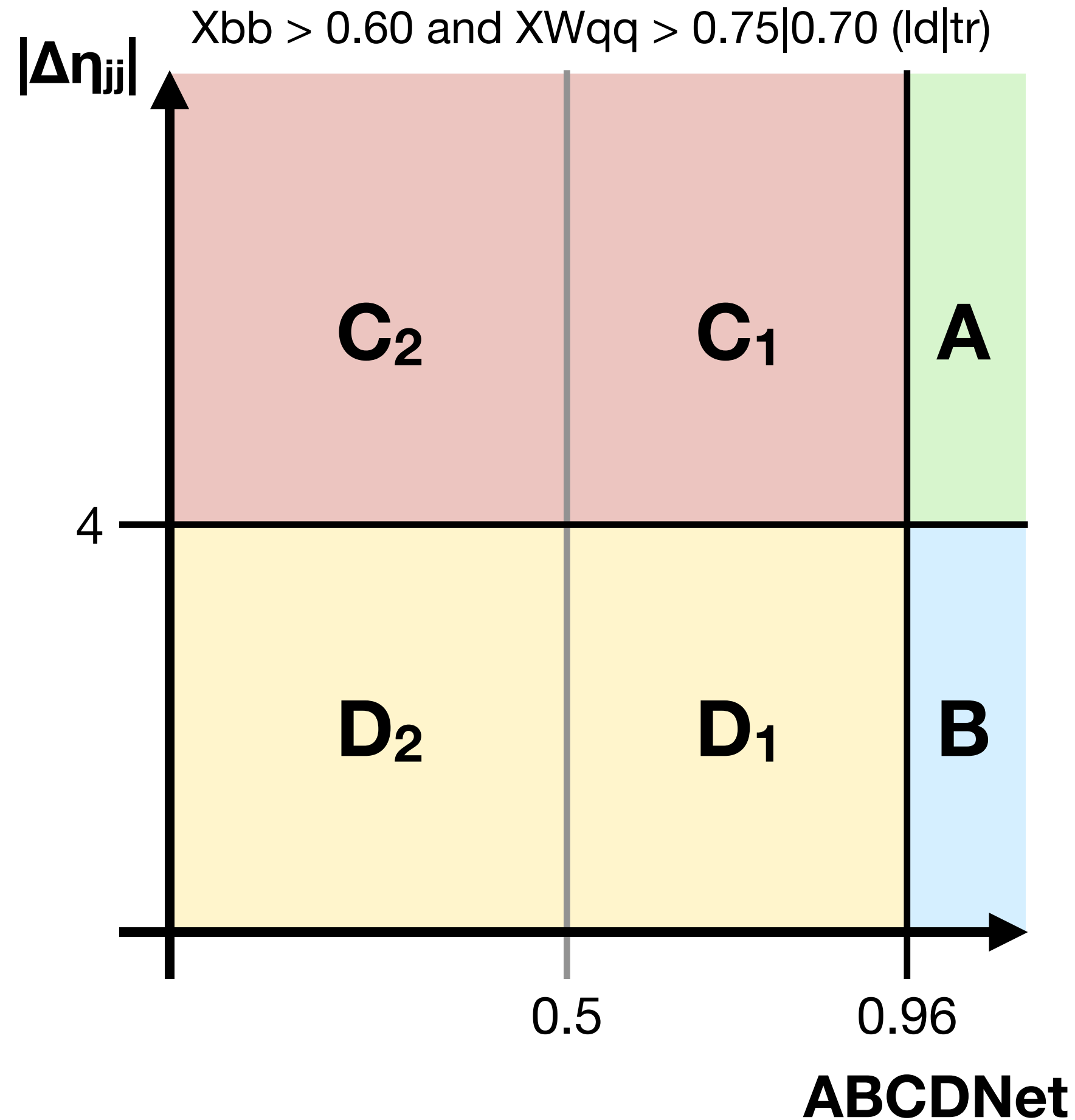
Expected sig. 3.73 ± 0.05

Predicted bkg. $0.93 \pm 0.47 \pm 0.28$

stat. syst.

Predicted significance ($S/\sqrt{B}$) is passable and the method closes in MC

Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	1.46	0.54	3.73	0.05	—	—
B	5.12	1.06	0.48	0.02	4	2.00
C	292.88	25.89	2.80	0.05	280	16.73
D	1012.4	41.07	0.63	0.02	1201	34.66

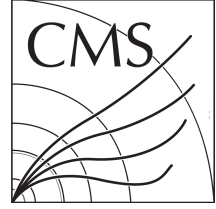
Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	1.46	0.54	3.73	0.05	—	—
B	5.12	1.06	0.48	0.02	4	2.00
C ₁	17.17	2.46	2.29	0.04	—	—
D ₁	81.2	9.25	0.47	0.02	70	8.37

**C₁ is signal polluted
⇒ can't unblind**

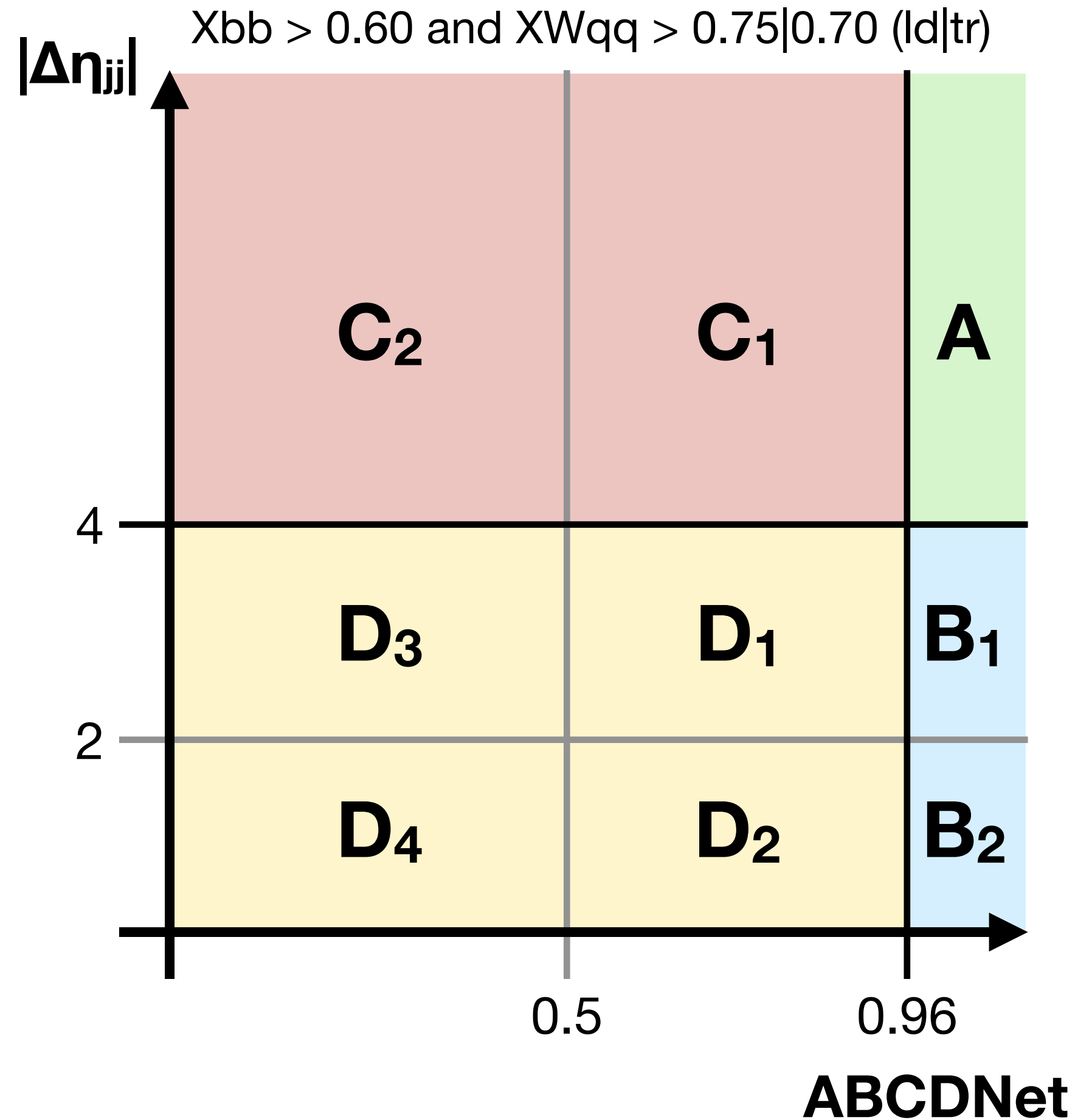
$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{bmatrix} 1.48 \pm 0.34 \text{ (MC)} \\ 0.93 \pm 0.47 \text{ (Data)} \end{bmatrix}$$

$$A^{\text{pred}} = B \times \frac{C_1}{D_1} = \begin{bmatrix} 1.08 \pm 0.30 \text{ (MC)} \\ ? \pm ? \text{ (Data)} \end{bmatrix}$$

ABCD works well with data in sidebands ⇒ method is valid!



Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	1.46	0.54	3.73	0.05	—	—
B	5.12	1.06	0.48	0.02	4	2.00
C	292.88	25.89	2.80	0.05	280	16.73
D	1012.4	41.07	0.63	0.02	1201	34.66

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	2.90	0.81	0.20	0.01	2	1.41
B ₂	2.22	0.68	0.28	0.01	2	1.41
D ₁	33.28	3.80	0.20	0.01	37	6.08
D ₂	47.87	8.44	0.27	0.01	33	5.74

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	33.28	3.80	0.20	0.01	37	6.08
D ₂	47.87	8.44	0.27	0.01	33	5.74
D ₃	441.29	28.47	0.07	0.01	540	23.24
D ₄	489.96	28.12	0.10	0.01	591	24.31

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	17.17	2.46	2.29	0.04	—	—
D ₁	33.28	3.80	0.20	0.01	37	6.08
C ₂	275.71	25.78	0.51	0.02	264	16.25
D ₃	441.29	28.47	0.07	0.01	540	23.24

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 1.48 \pm 0.34 \text{ (MC)} \\ \mathbf{0.93 \pm 0.47 \text{ (Data)}} \end{cases}$$

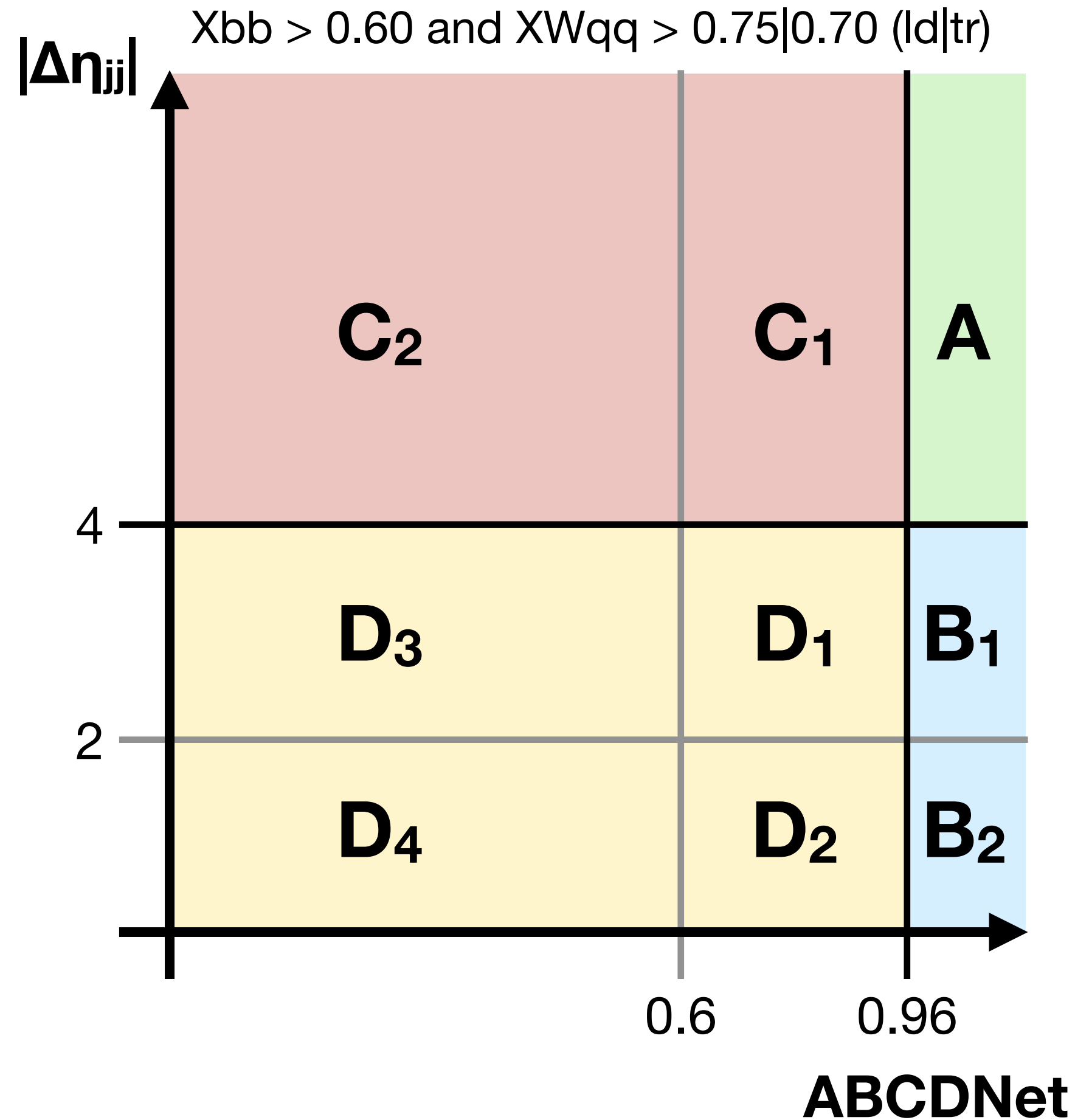
$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = \mathbf{2.24 \pm 1.67 \text{ (Data) } \checkmark}$$

$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = \mathbf{30.15 \pm 5.55 \text{ (Data) } \checkmark}$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = \mathbf{C1 \text{ is signal polluted} \Rightarrow \text{can't unblind}}$$

ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	1.46	0.54	3.73	0.05	—	—
B	5.12	1.06	0.48	0.02	4	2.00
C	292.88	25.89	2.80	0.05	280	16.73
D	1012.4	41.07	0.63	0.02	1201	34.66

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	2.90	0.81	0.20	0.01	2	1.41
B ₂	2.22	0.68	0.28	0.01	2	1.41
D ₁	27.26	3.48	0.18	0.01	30	5.48
D ₂	37.87	8.14	0.24	0.01	26	5.10

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	27.26	3.48	0.18	0.01	30	5.48
D ₂	37.87	8.14	0.24	0.01	26	5.10
D ₃	447.31	28.51	0.09	0.01	547	23.39
D ₄	499.96	28.21	0.12	0.01	598	24.45

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	14.91	2.33	2.15	0.04	—	—
D ₁	27.26	3.48	0.18	0.01	30	5.48
C ₂	277.97	25.79	0.64	0.02	269	16.40
D ₃	447.31	28.51	0.09	0.01	547	23.39

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 1.48 \pm 0.34 \text{ (MC)} \\ \mathbf{0.93 \pm 0.47 \text{ (Data)}} \end{cases}$$

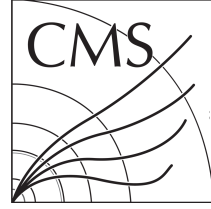
$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = \mathbf{2.31 \pm 1.75 \text{ (Data) } \checkmark}$$

$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = \mathbf{23.78 \pm 4.87 \text{ (Data) } \checkmark}$$

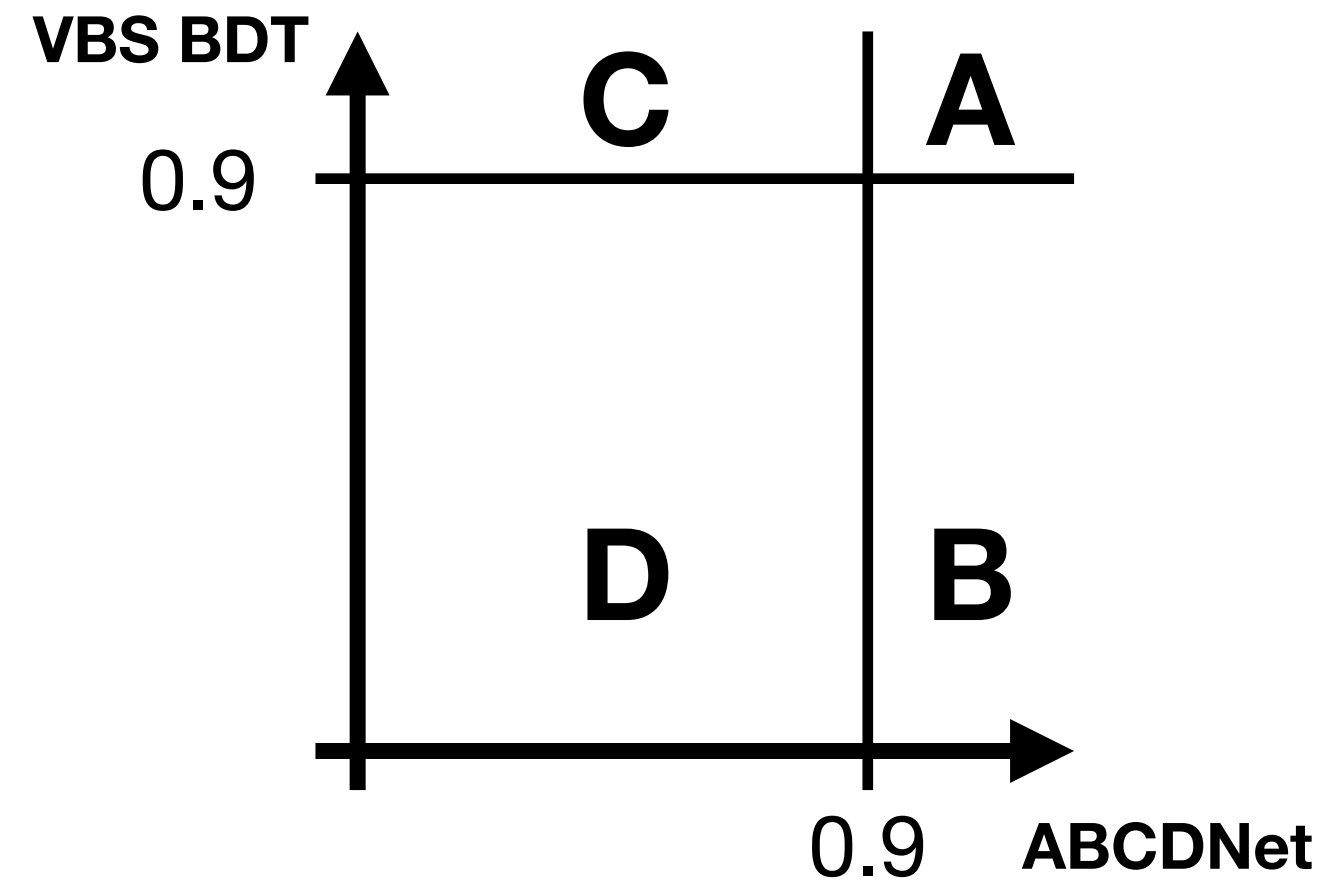
$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = \mathbf{C1 \text{ is signal polluted} \Rightarrow \text{can't unblind}}$$

ABCD works well with data in sidebands $\Rightarrow$ method is valid!

ABCD: ABCDNet vs. VBS BDT



ABCD Configuration & MC Closure



$X_{bb} > 0.8$ and $X_{Wqq} > 0.6|0.4$ (l|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A	0.72	0.28	3.80	0.05	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B	40.56	3.52	2.71	0.05	44	6.63
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	48.72	7.89	1.38	0.03	80	8.94
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	3025.85	79.24	1.30	0.03	3243	56.95

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{0.65 \pm 0.12}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{1.09 \pm 0.20}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{0.69}} \sqrt{\left(\frac{\mathbf{0.28}}{\mathbf{0.72}}\right)^2 + \left(\frac{\mathbf{0.12}}{\mathbf{0.65}}\right)^2} = 62.9\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 18.9\%$$

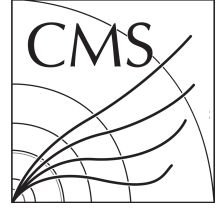
Final Result

Expected sig. 3.80 ± 0.05

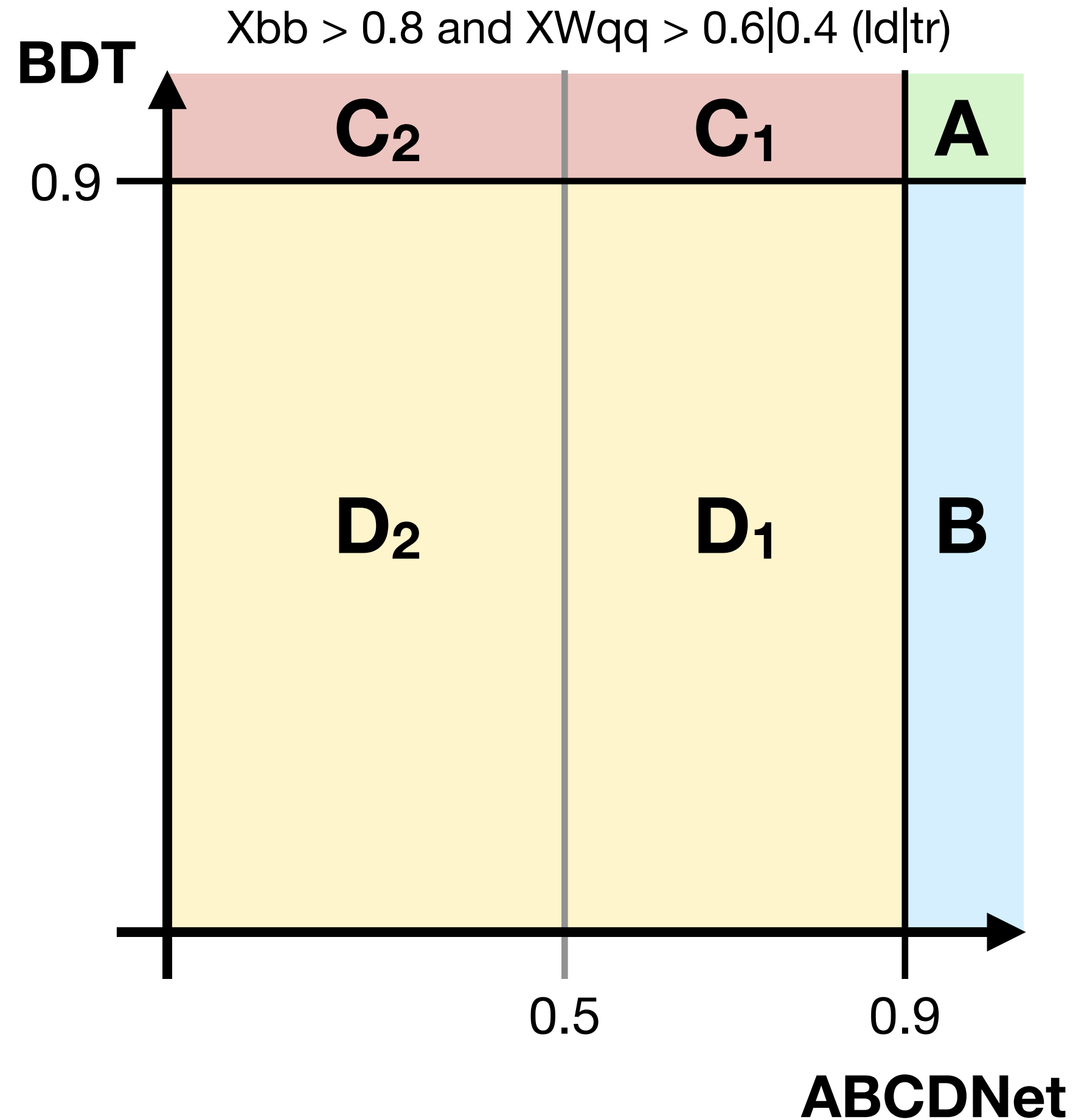
Predicted bkg. $1.09 \pm 0.20 \pm 0.68$

stat. syst.

Predicted significance ($S/\sqrt{B}$) is passable and the method closes in MC



Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.72	0.28	3.80	0.05	—	—
B	40.56	3.52	2.71	0.05	44	6.63
C	48.72	7.89	1.38	0.03	80	8.94
D	3025.8	79.24	1.30	0.03	3243	56.95

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.72	0.28	3.80	0.05	—	—
B	40.56	3.52	2.71	0.05	44	6.63
C ₁	2.63	0.95	1.01	0.03	—	—
D ₁	199.4	13.27	0.84	0.03	183	13.53

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	2.63	0.95	1.01	0.03	—	—
D ₁	199.43	13.27	0.84	0.03	183	13.53
C ₂	46.09	7.83	0.37	0.02	76	8.72
D ₂	2826.42	78.12	0.46	0.02	3060	55.32

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{bmatrix} 0.65 \pm 0.12 \text{ (MC)} \\ 1.09 \pm 0.20 \text{ (Data)} \end{bmatrix}$$

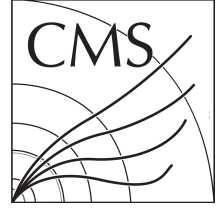
$$A^{\text{pred}} = B \times \frac{C_1}{D_1} = \begin{bmatrix} 0.54 \pm 0.20 \text{ (MC)} \\ ? \pm ? \text{ (Data)} \end{bmatrix}$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = 4.55 \pm 0.63 \text{ (Data) ?}$$

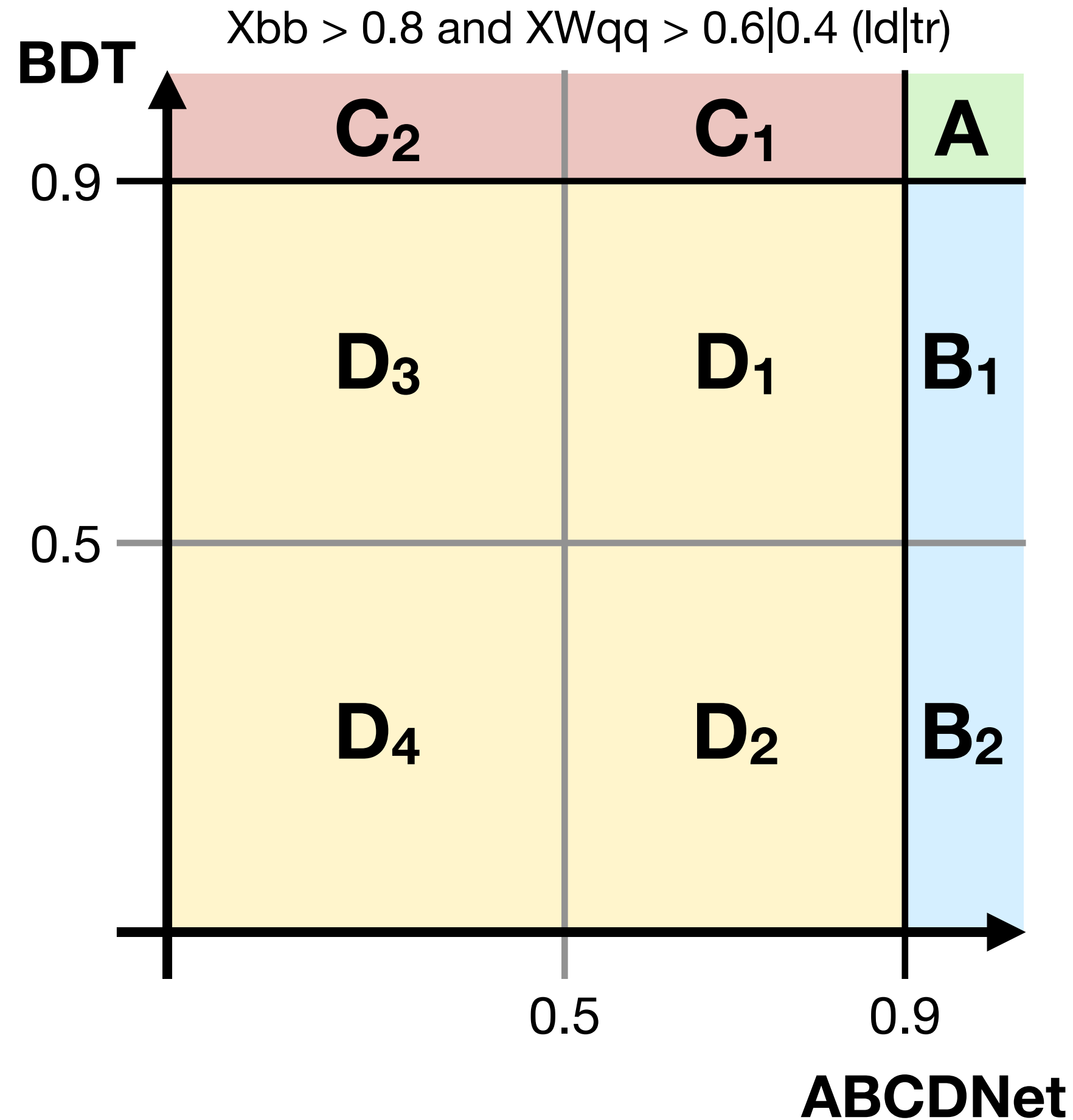
ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

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Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.72	0.28	3.80	0.05	—	—
B	40.56	3.52	2.71	0.05	44	6.63
C	48.72	7.89	1.38	0.03	80	8.94
D	3025.85	79.24	1.30	0.03	3243	56.95

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	4.94	1.06	1.92	0.04	—	—
B ₂	35.62	3.36	0.79	0.02	39	6.24
D ₁	18.94	2.93	0.56	0.02	21	4.58
D ₂	180.48	12.95	0.28	0.01	162	12.73

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	18.94	2.93	0.56	0.02	21	4.58
D ₂	180.48	12.95	0.28	0.01	162	12.73
D ₃	279.77	20.77	0.24	0.01	320	17.89
D ₄	2546.65	75.31	0.21	0.01	2740	52.35

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	2.63	0.95	1.01	0.03	—	—
D ₁	18.94	2.93	0.56	0.02	21	4.58
C ₂	46.09	7.83	0.37	0.02	76	8.72
D ₃	279.77	20.77	0.24	0.01	320	17.89

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 0.65 \pm 0.12 \text{ (MC)} \\ 1.09 \pm 0.20 \text{ (Data)} \end{cases}$$

$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = 5.06 \pm 1.42 \text{ (Data) ?}$$

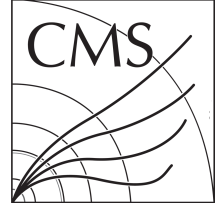
$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = 18.92 \pm 1.86 \text{ (Data) } \checkmark$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = 4.99 \pm 1.26 \text{ (Data) ?}$$

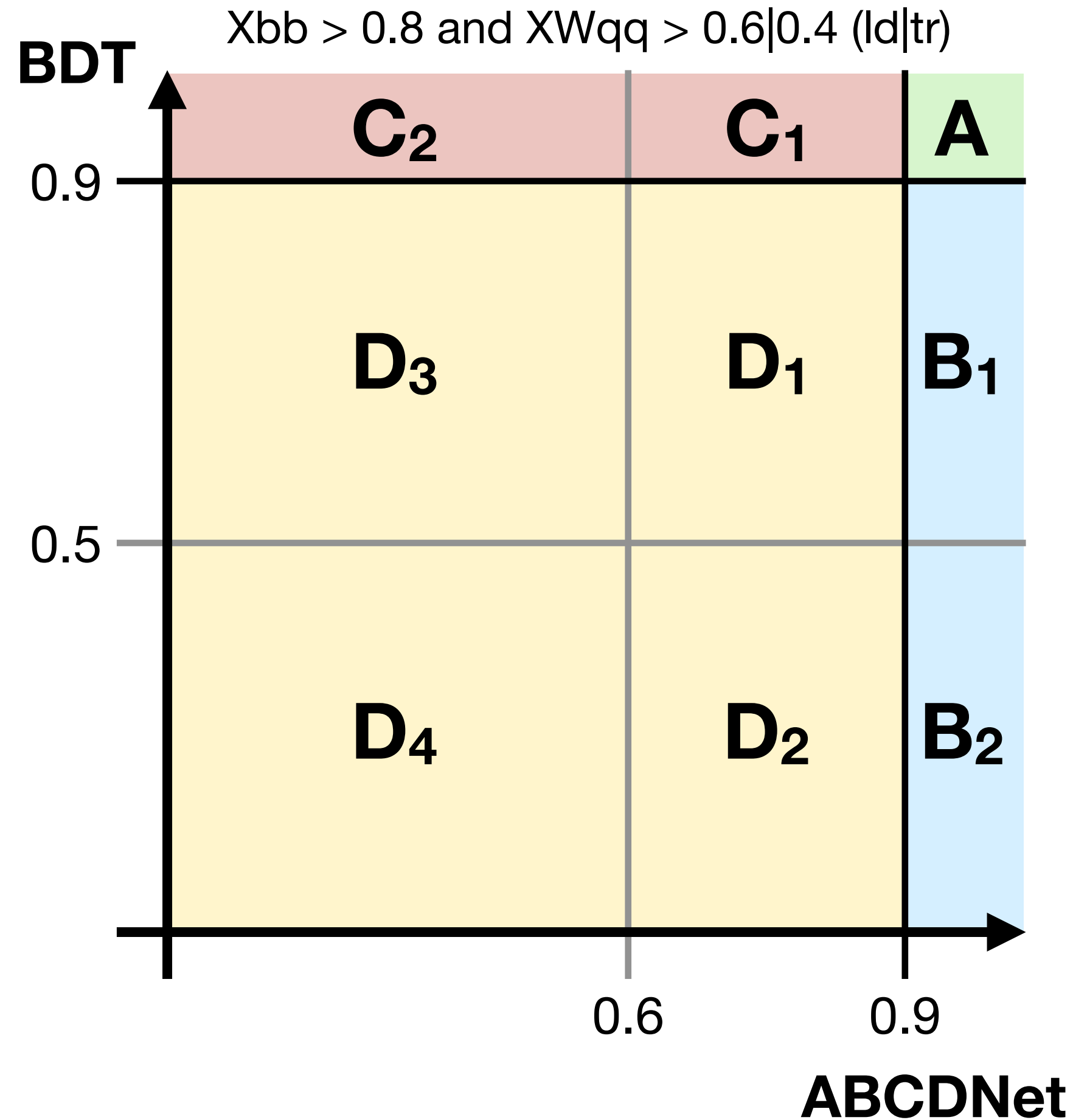
ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

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Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.72	0.28	3.80	0.05	—	—
B	40.56	3.52	2.71	0.05	44	6.63
C	48.72	7.89	1.38	0.03	80	8.94
D	3025.85	79.24	1.30	0.03	3243	56.95

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	4.94	1.06	1.92	0.04	—	—
B ₂	35.62	3.36	0.79	0.02	39	6.24
D ₁	12.46	2.24	0.50	0.02	15	3.87
D ₂	130.54	12.00	0.24	0.01	120	10.95

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	12.46	2.24	0.50	0.02	15	3.87
D ₂	130.54	12.00	0.24	0.01	120	10.95
D ₃	286.26	20.86	0.30	0.02	326	18.06
D ₄	2596.59	75.47	0.25	0.01	2782	52.74

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	2.09	0.88	0.91	0.03	—	—
D ₁	12.46	2.24	0.50	0.02	15	3.87
C ₂	46.63	7.84	0.47	0.02	77	8.77
D ₃	286.26	20.86	0.30	0.02	326	18.06

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 0.65 \pm 0.12 \text{ (MC)} \\ 1.09 \pm 0.20 \text{ (Data)} \end{cases}$$

$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = 4.88 \pm 1.55 \text{ (Data) ?}$$

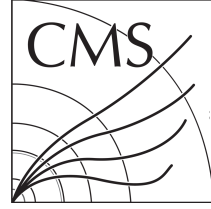
$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = 14.06 \pm 1.52 \text{ (Data) } \checkmark$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = 3.54 \pm 1.02 \text{ (Data) ?}$$

ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

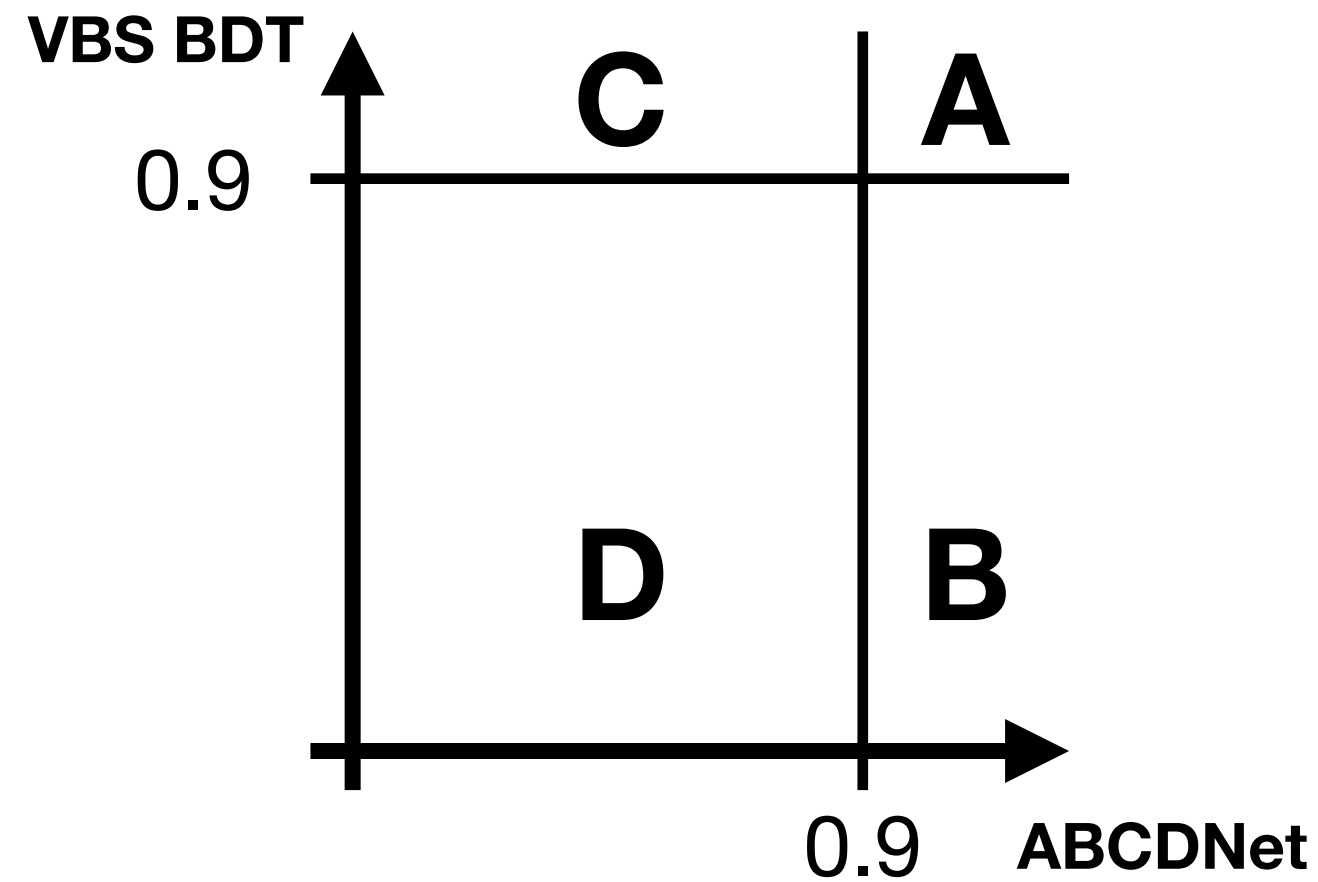
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Closure in Xbb Sideband

$X_{bb} \leq 0.80$ and $X_{Wqq} > 0.60|0.40$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A	1.18	0.64	0.29	0.01	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B	39.35	3.99	0.25	0.01	49	7.0
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	49.98	10.74	0.27	0.01	58	7.6
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	2552.26	73.17	0.24	0.01	2746	52.4



$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{0.77 \pm 0.18}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{1.03 \pm 0.20}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{0.97}} \sqrt{\left(\frac{\mathbf{0.64}}{\mathbf{1.18}}\right)^2 + \left(\frac{\mathbf{0.18}}{\mathbf{0.77}}\right)^2} = 61.1\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 19.5\%$$

Final Result

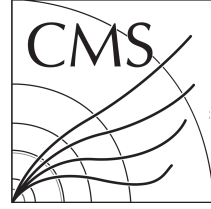
Expected sig. 0.29 ± 0.01

Predicted bkg. $1.03 \pm 0.20 \pm 0.63$

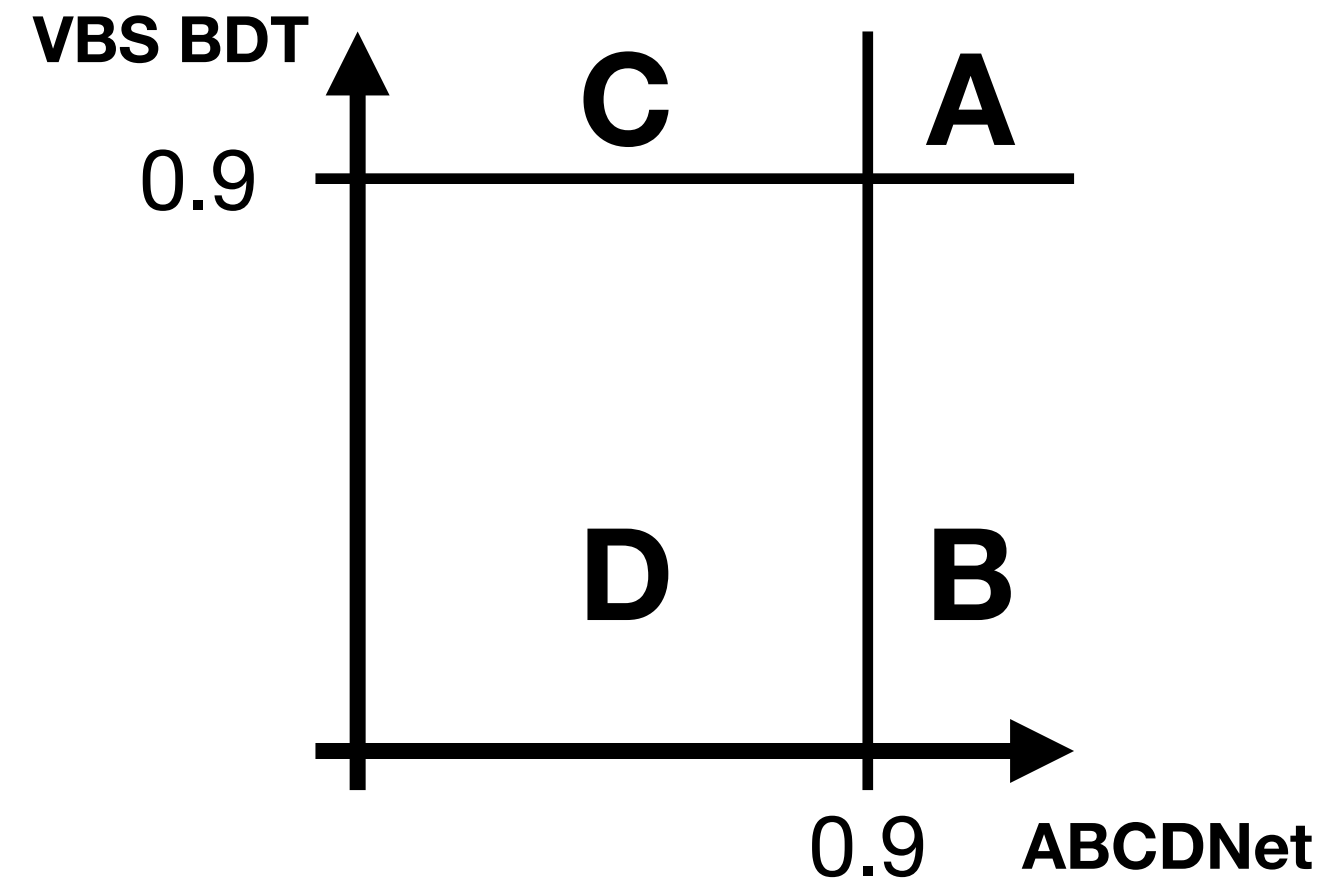
stat.

syst.

Method closes for data in ParticleNet sideband



Closure in ParticleNet Sideband



$X_{bb} \leq 0.80$ or $X_{Wqq} \leq 0.60|0.40$ ($l_d|tr$)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A	4.02	1.19	0.75	0.02	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B	155.80	7.75	0.59	0.02	155	12.4
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	237.20	24.86	0.55	0.02	211	14.5
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	10832.14	162.63	0.64	0.02	10609	103.0

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = 3.41 \pm 0.40$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = 3.08 \pm 0.33$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{3.71} \sqrt{\left(\frac{1.19}{4.02}\right)^2 + \left(\frac{0.40}{3.41}\right)^2} = 8.6\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 10.6\%$$

Final Result

Expected sig. 0.75 ± 0.02

Predicted bkg. $3.08 \pm 0.33 \pm 0.26$

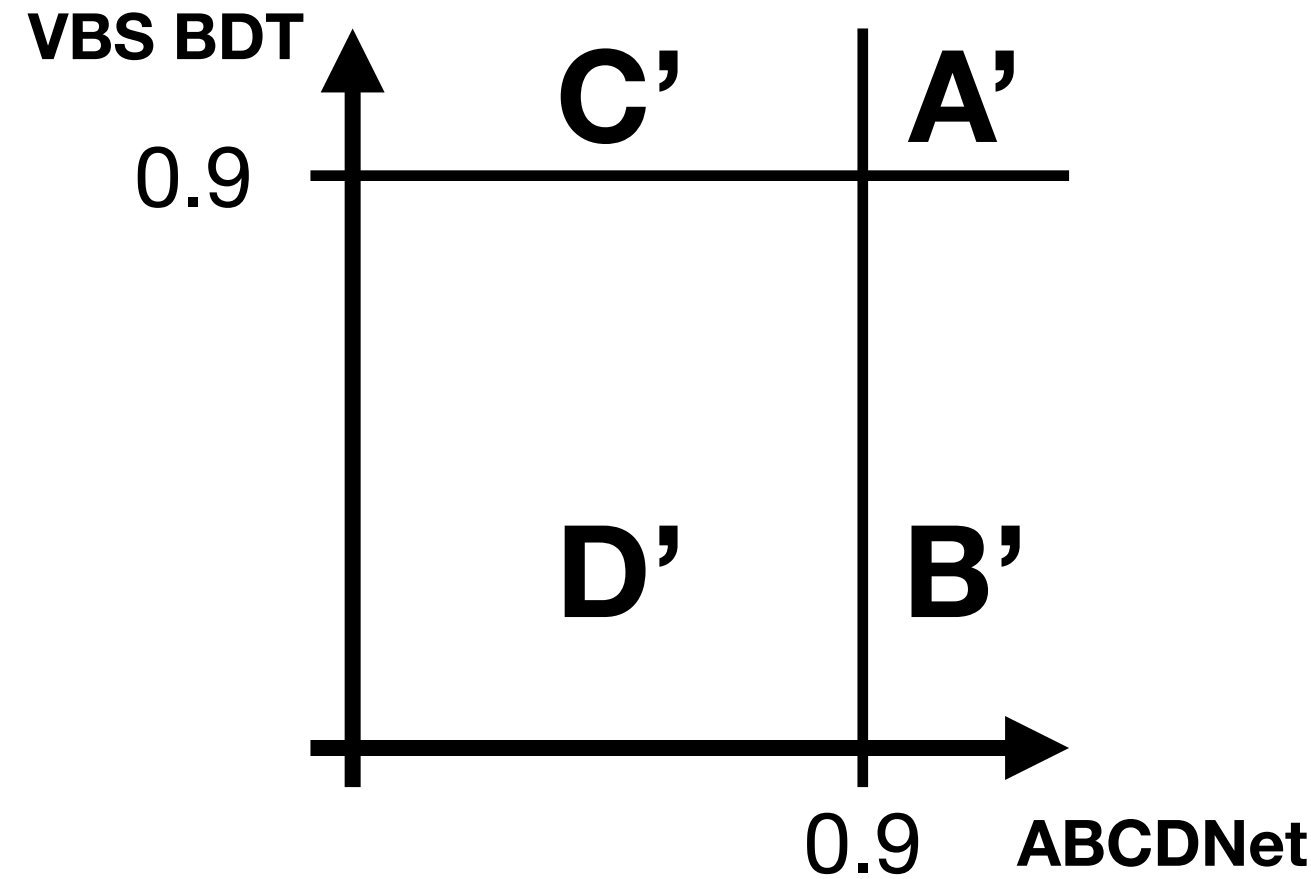
stat.

syst.

Method closes for data in ParticleNet sideband

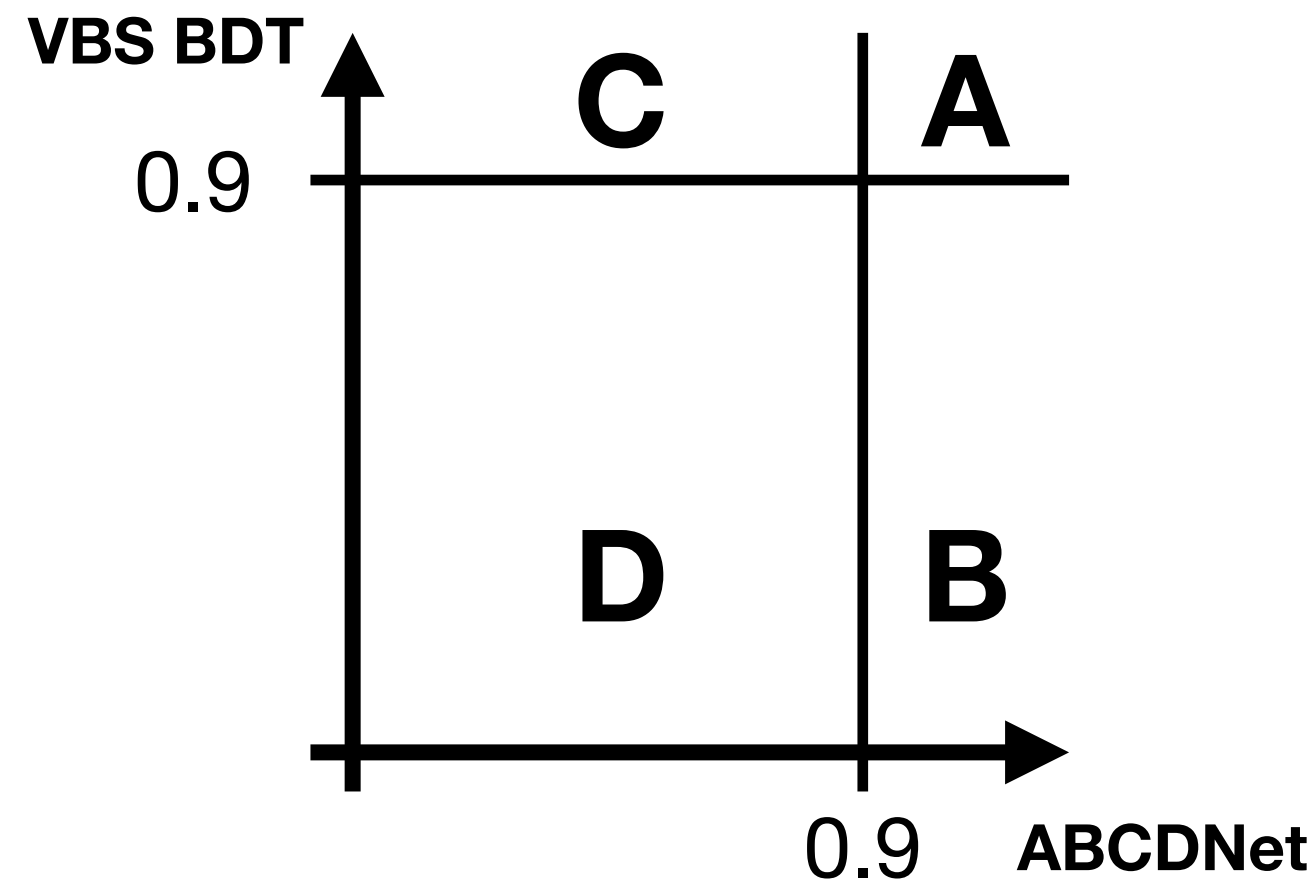


Closure in ParticleNet Sideband



$X_{bb} \leq 0.80$ or $X_{Wqq} \leq 0.60|0.40$ ($|d|tr$)

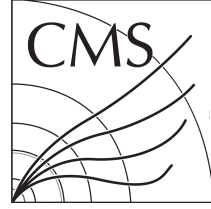
Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A'	4.02	1.19	0.75	0.02	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B'	155.80	7.75	0.59	0.02	155	12.4
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C'	237.20	24.86	0.55	0.02	211	14.5
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D'	10832.14	162.63	0.64	0.02	10609	103.0



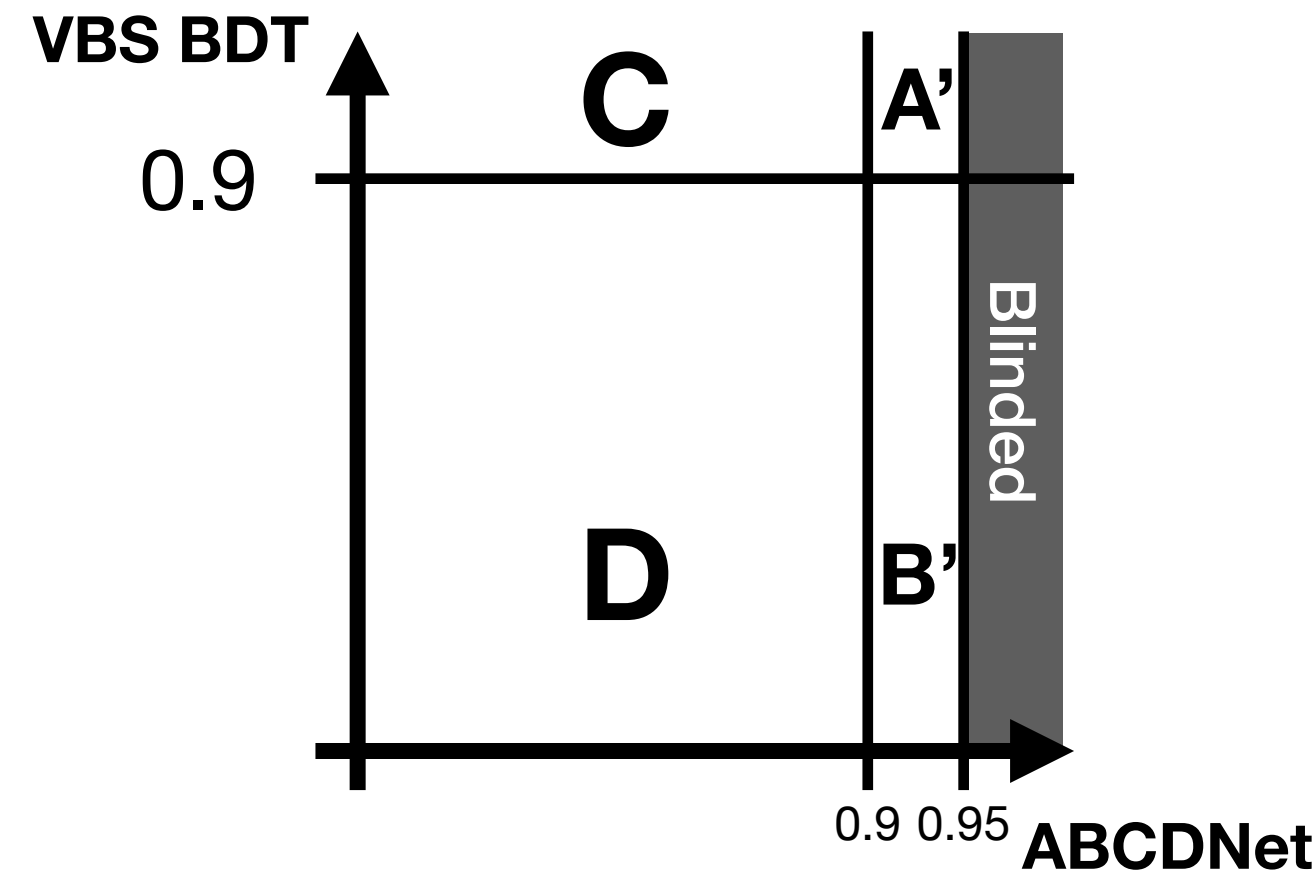
$X_{bb} > 0.8$ and $X_{Wqq} > 0.6|0.4$ ($|d|tr$)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A	0.72	0.28	3.80	0.05	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B	40.56	3.52	2.71	0.05	44	6.63
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	48.72	7.89	1.38	0.03	80	8.94
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	3025.85	79.24	1.30	0.03	3243	56.95

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A'/A	5.54	2.72	5.08	0.18	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B'/B	3.84	0.38	4.58	0.18	3.5	0.60
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C'/C	4.87	0.94	2.51	0.11	2.6	0.35
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D'/D	3.58	0.11	2.03	0.09	3.3	0.07



Closure in PNet + ABCDNet Sideband



$X_{bb} \leq 0.80$ or $X_{Wqq} \leq 0.60|0.40$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A'	2.05	0.92	0.16	0.01	1	1.00
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B'	83.00	5.84	0.16	0.01	79	8.9
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	237.20	24.86	0.55	0.02	211	14.5
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	10832.14	162.63	0.64	0.02	10609	103.0

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{1.82 \pm 0.23}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{1.57 \pm 0.21}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{1.93}} \sqrt{\left(\frac{\mathbf{0.92}}{\mathbf{2.05}}\right)^2 + \left(\frac{\mathbf{0.23}}{\mathbf{1.82}}\right)^2} = 24.3\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 13.2\%$$

Final Result

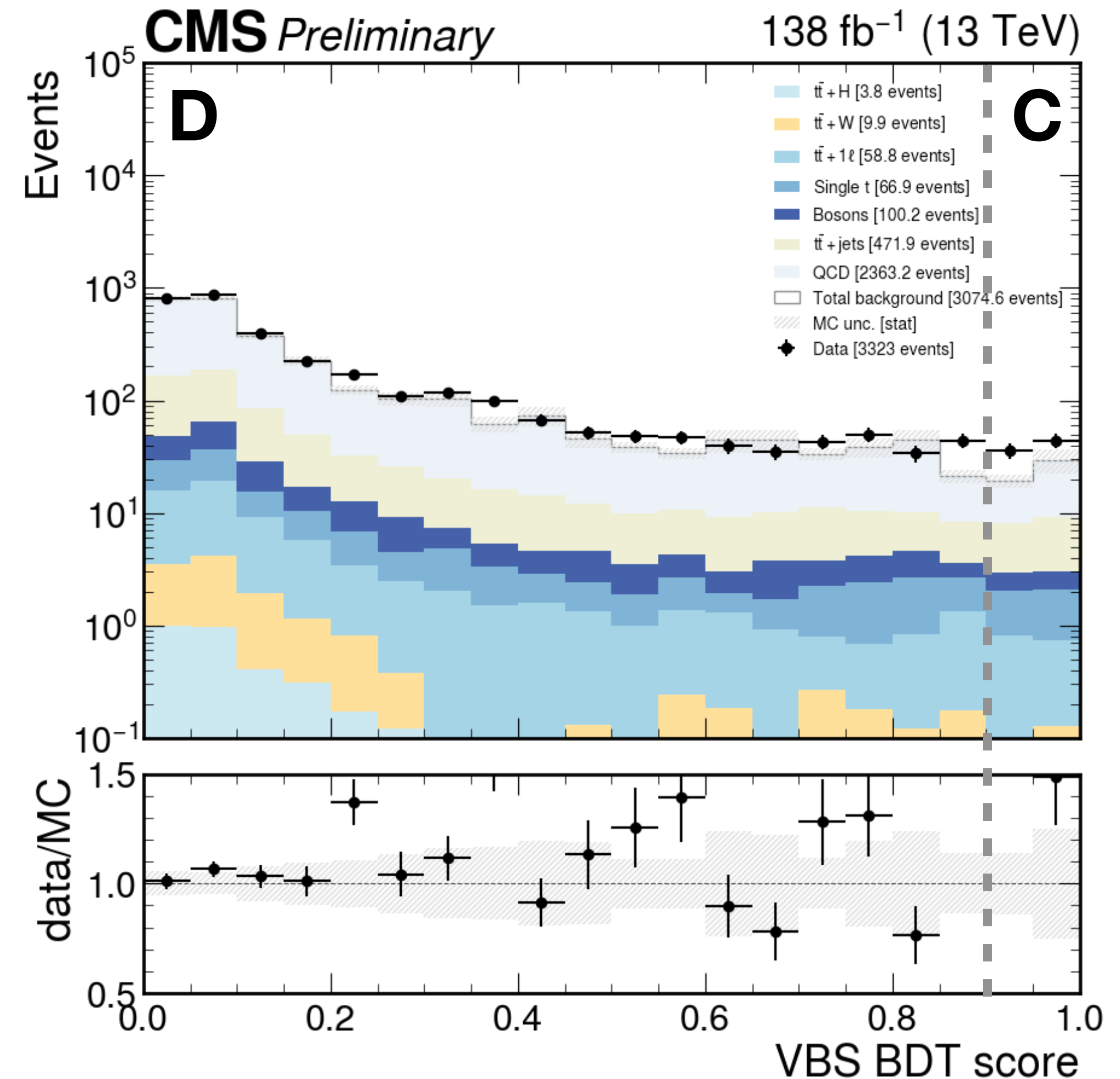
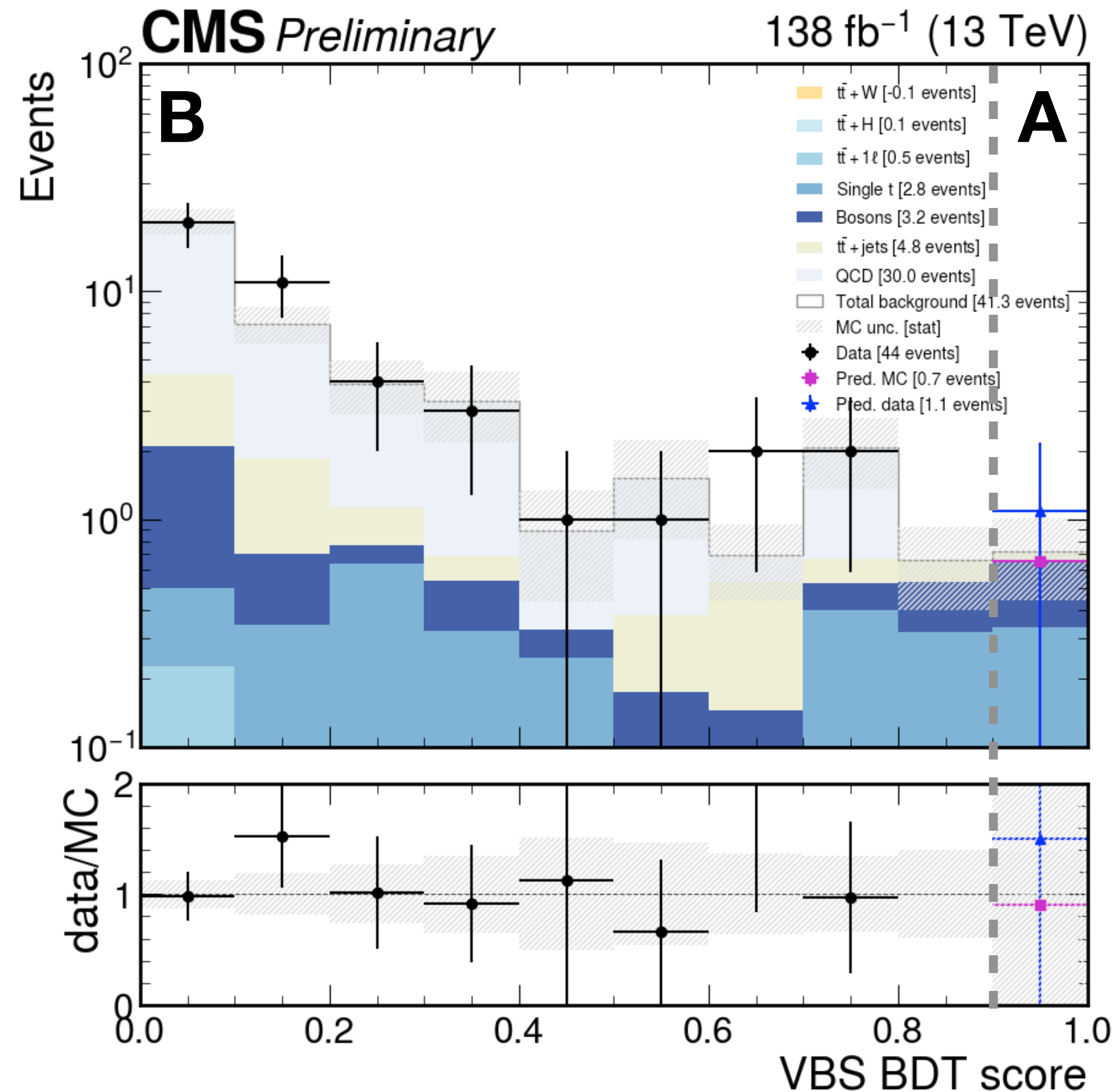
Expected sig. 0.16 ± 0.01

Predicted bkg. $1.57 \pm 0.21 \pm 0.38$

stat. *syst.*

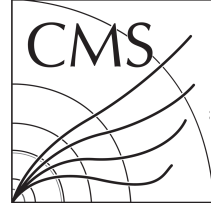
Method closes for data in ParticleNet sideband

Reweighted vs. Single-point

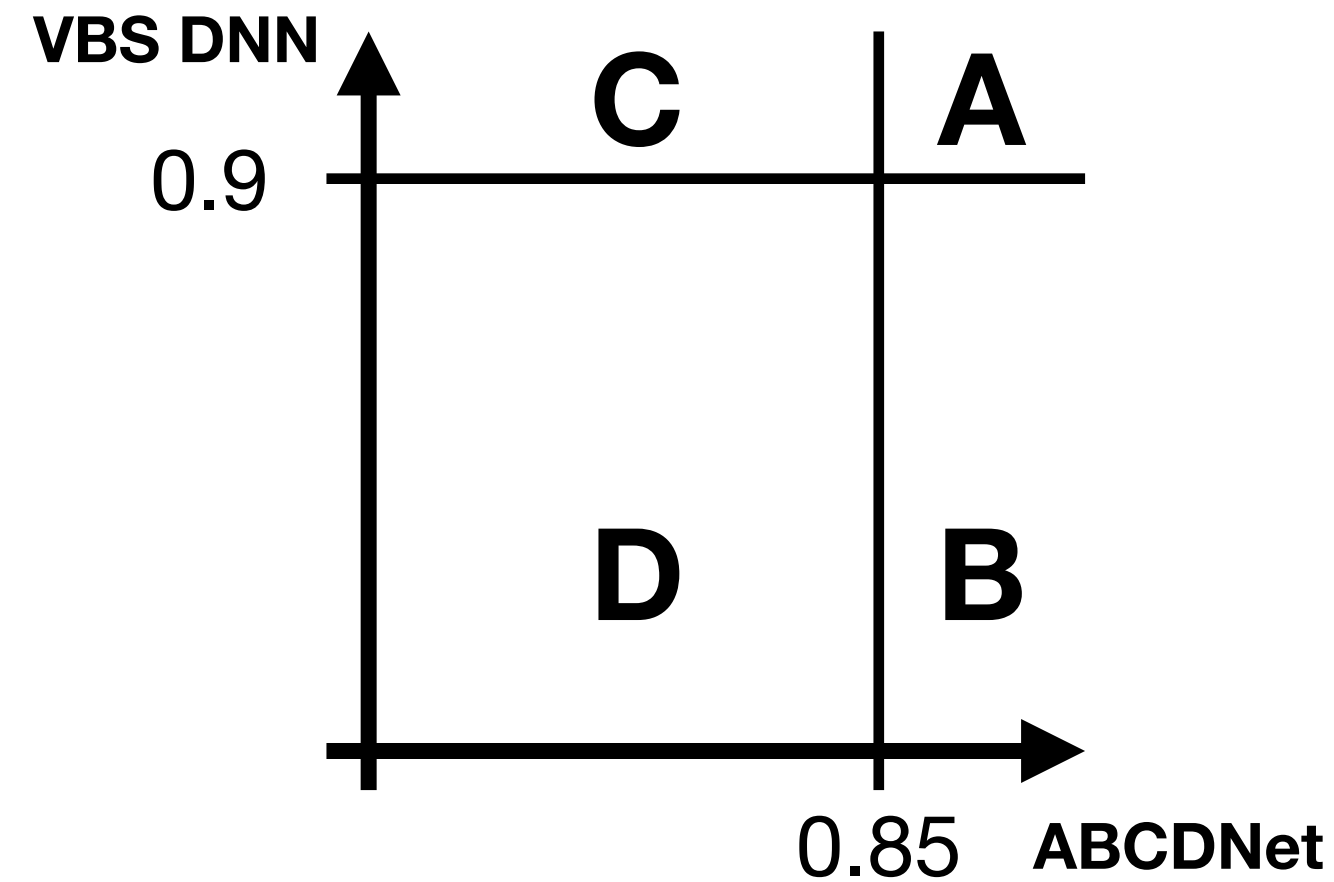


No obvious systematic issues in data/MC

ABCD: ABCDNet vs. VBS DNN



ABCD Configuration & MC Closure



$X_{bb} > 0.5$ and $X_{Wqq} > 0.5|0.4$ (l|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS DNN > 0.9 and ABCDNet > 0.9	A	0.95	0.37	6.88	0.07	—	—
VBS DNN ≤ 0.9 and ABCDNet > 0.9	B	189.89	8.37	0.92	0.03	185	13.60
VBS DNN > 0.9 and ABCDNet ≤ 0.9	C	56.11	2.29	2.35	0.04	33	5.74
VBS DNN ≤ 0.9 and ABCDNet ≤ 0.9	D	7271.69	125.39	0.54	0.02	7817	88.41

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{1.47 \pm 0.09}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{0.78 \pm 0.15}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{1.21}} \sqrt{\left(\frac{\mathbf{0.37}}{\mathbf{0.95}}\right)^2 + \left(\frac{\mathbf{0.09}}{\mathbf{1.47}}\right)^2} = 32.9\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 18.9\%$$

Final Result

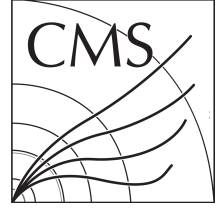
Expected sig. 6.88 ± 0.07

Predicted bkg. $0.78 \pm 0.15 \pm 0.26$

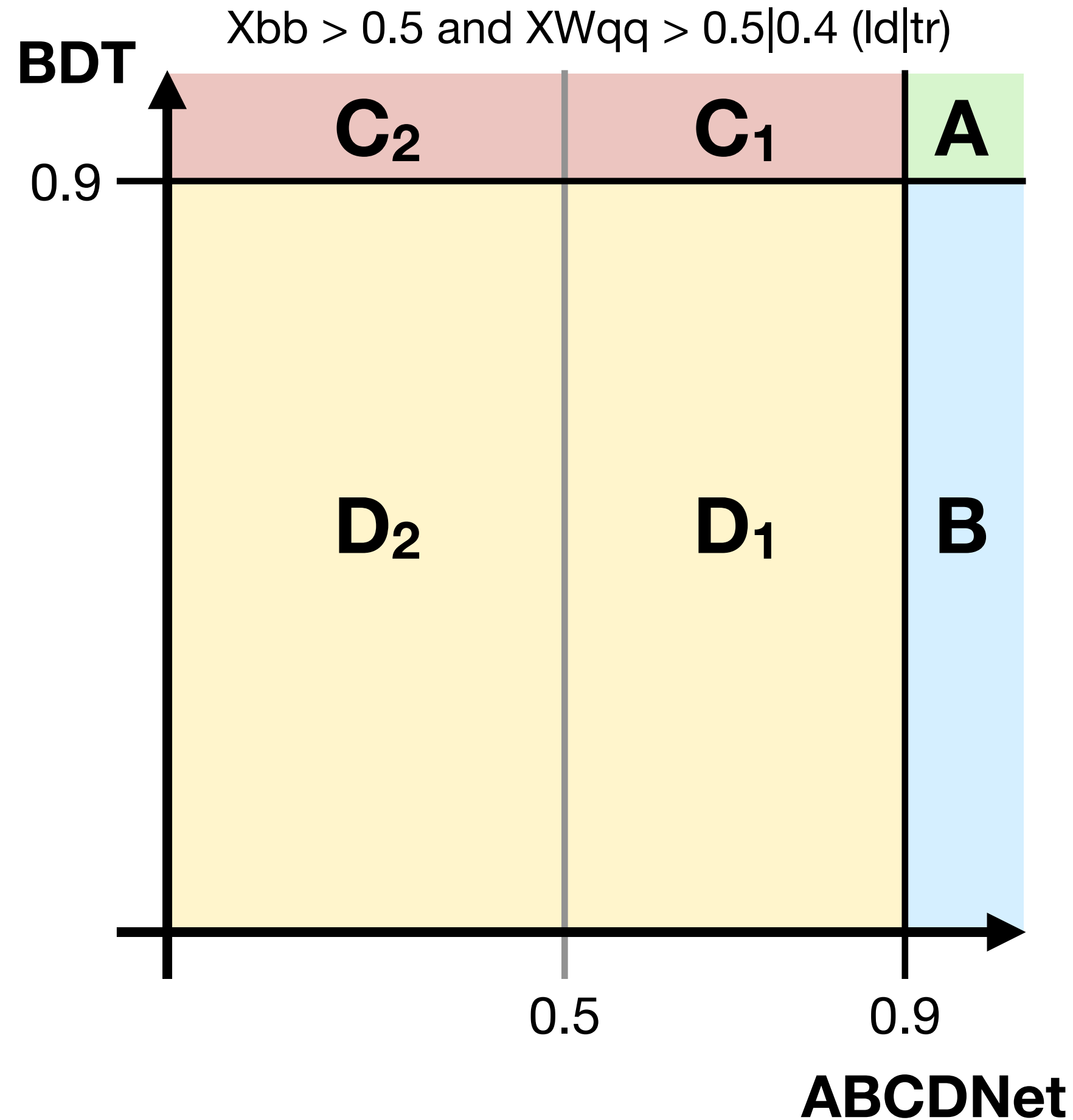
stat.

syst.

Predicted significance ($S/\sqrt{B}$) is very good and the method roughly closes in MC



Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.95	0.37	6.88	0.07	—	—
B	189.89	8.37	0.92	0.03	185	13.60
C	56.11	2.29	2.35	0.04	33	5.74
D	7271.7	125.39	0.54	0.02	7817	88.41

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.95	0.37	6.88	0.07	—	—
B	189.89	8.37	0.92	0.03	185	13.60
C ₁	3.18	0.48	1.52	0.03	—	—
D ₁	570.3	24.36	0.27	0.01	552	23.49

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	3.18	0.48	1.52	0.03	—	—
D ₁	570.27	24.36	0.27	0.01	552	23.49
C ₂	52.94	2.23	0.83	0.02	31	5.57
D ₂	6701.42	123.00	0.27	0.01	7265	85.23

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{bmatrix} 1.47 \pm 0.09 \text{ (MC)} \\ 0.78 \pm 0.15 \text{ (Data)} \end{bmatrix} \sim$$

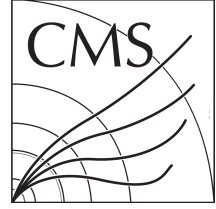
$$A^{\text{pred}} = B \times \frac{C_1}{D_1} = \begin{bmatrix} 1.06 \pm 0.17 \text{ (MC)} \\ ? \pm ? \text{ (Data)} \end{bmatrix}$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = \mathbf{2.36 \pm 0.44 \text{ (Data) ?}}$$

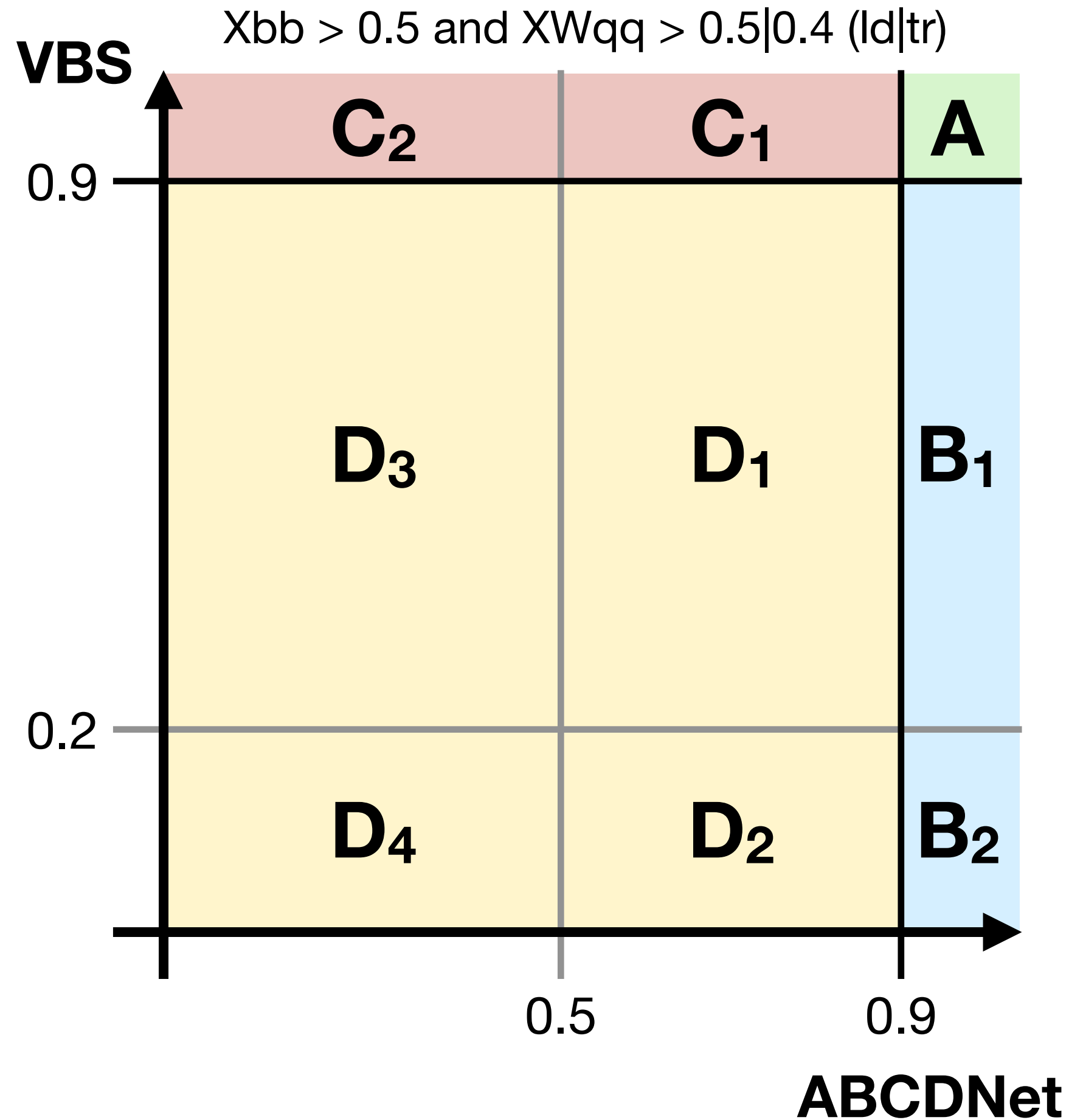
ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

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Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.95	0.37	6.88	0.07	—	—
B	189.89	8.37	0.92	0.03	185	13.60
C	56.11	2.29	2.35	0.04	33	5.74
D	7271.69	125.39	0.54	0.02	7817	88.41

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	11.22	1.33	0.87	0.03	7	2.65
B ₂	178.66	8.26	0.05	0.01	178	13.34
D ₁	42.61	3.12	0.26	0.01	29	5.39
D ₂	527.67	24.15	0.01	0.00	523	22.87

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	42.61	3.12	0.26	0.01	29	5.39
D ₂	527.67	24.15	0.01	0.00	523	22.87
D ₃	514.84	14.30	0.25	0.01	380	19.49
D ₄	6186.57	122.16	0.02	0.00	6885	82.98

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	3.18	0.48	1.52	0.03	—	—
D ₁	42.61	3.12	0.26	0.01	29	5.39
C ₂	52.94	2.23	0.83	0.02	31	5.57
D ₃	514.84	14.30	0.25	0.01	380	19.49

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 1.47 \pm 0.09 \text{ (MC)} \\ \mathbf{0.78 \pm 0.15 \text{ (Data)}} \end{cases}$$

$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = \mathbf{9.87 \pm 2.02 \text{ (Data) } \checkmark}$$

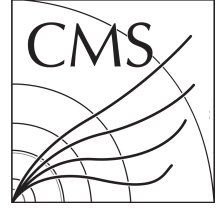
$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = \mathbf{28.87 \pm 1.98 \text{ (Data) } \checkmark}$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = \mathbf{2.37 \pm 0.62 \text{ (Data) ?}}$$

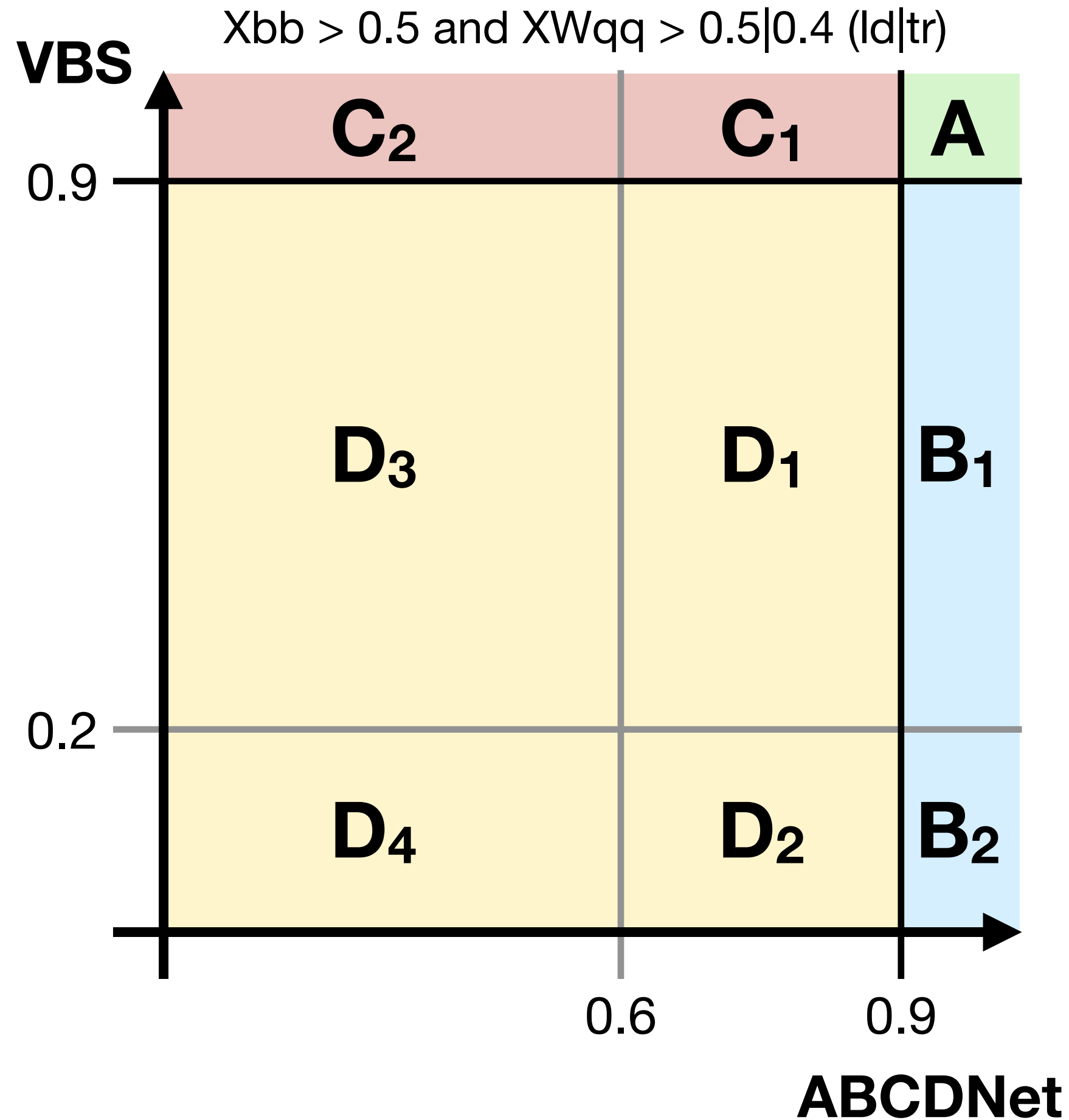
ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

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Closure in Sidebands



Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
A	0.95	0.37	6.88	0.07	—	—
B	189.89	8.37	0.92	0.03	185	13.60
C	56.11	2.29	2.35	0.04	33	5.74
D	7271.69	125.39	0.54	0.02	7817	88.41

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
B ₁	11.22	1.33	0.87	0.03	7	2.65
B ₂	178.66	8.26	0.05	0.01	178	13.34
D ₁	28.31	2.45	0.21	0.01	19	4.36
D ₂	333.99	14.65	0.01	0.00	355	18.84

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
D ₁	28.31	2.45	0.21	0.01	19	4.36
D ₂	333.99	14.65	0.01	0.00	355	18.84
D ₃	529.14	14.43	0.30	0.02	390	19.75
D ₄	6380.25	123.66	0.02	0.00	7053	83.98

Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
C ₁	2.42	0.43	1.29	0.03	—	—
D ₁	28.31	2.45	0.21	0.01	19	4.36
C ₂	53.69	2.24	1.05	0.03	31	5.57
D ₃	529.14	14.43	0.30	0.02	390	19.75

$$A^{\text{pred}} = B \times \frac{C}{D} = \begin{cases} 1.47 \pm 0.09 \text{ (MC)} \\ \mathbf{0.78 \pm 0.15 \text{ (Data)}} \end{cases}$$

$$B_1^{\text{pred}} = B_2 \times \frac{D_1}{D_2} = \mathbf{9.53 \pm 2.35 \text{ (Data) } \checkmark}$$

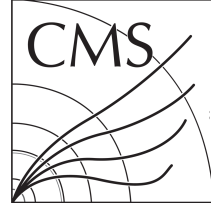
$$D_1^{\text{pred}} = D_2 \times \frac{D_3}{D_4} = \mathbf{19.63 \pm 1.46 \text{ (Data) } \checkmark}$$

$$C_1^{\text{pred}} = D_1 \times \frac{C_2}{D_3} = \mathbf{1.51 \pm 0.45 \text{ (Data) ?}}$$

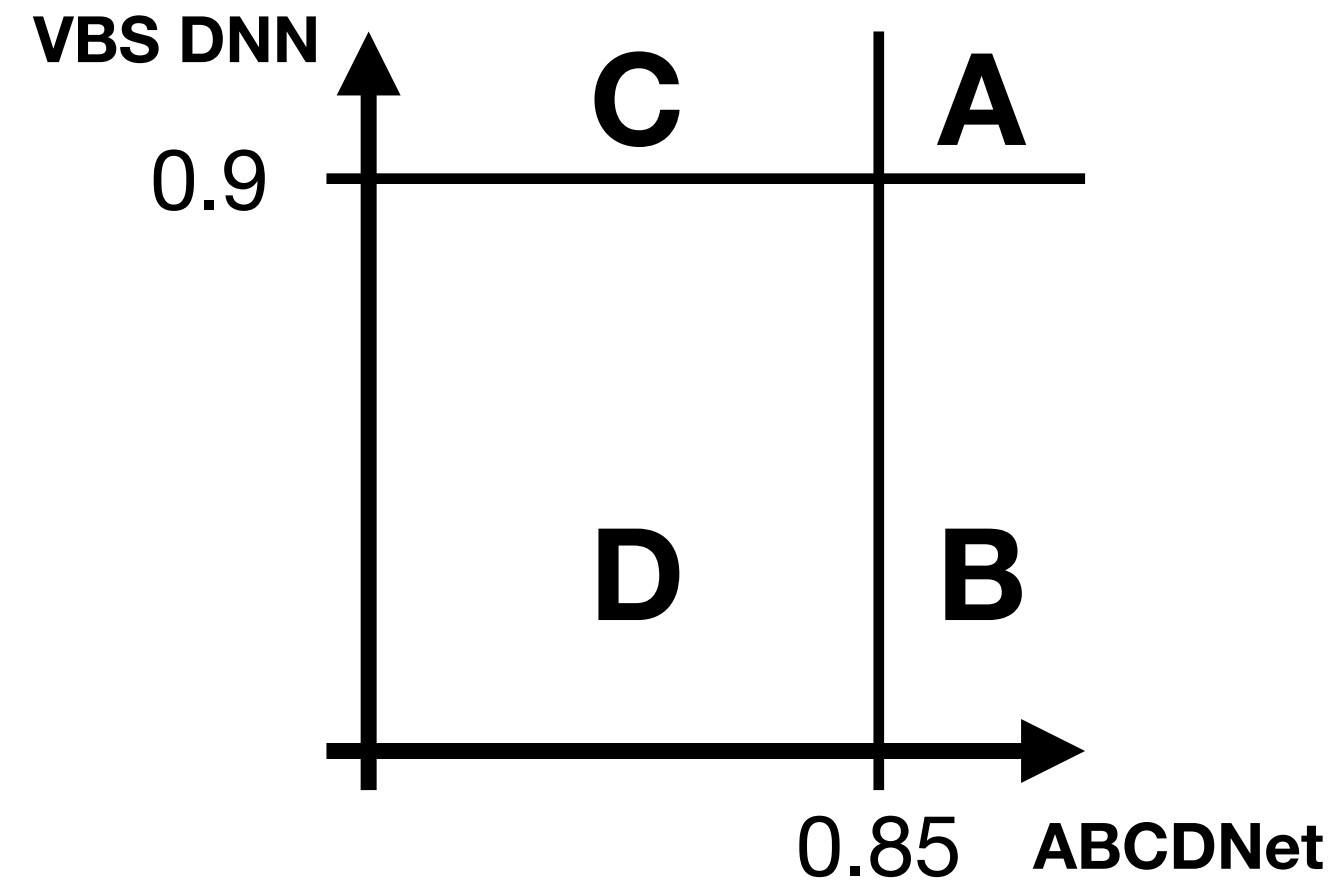
ABCD works well with data in sidebands $\Rightarrow$ method is valid!

Epoch = 600 | LR = 0.001 (constant) | $\lambda = 30$ | QCD norm | All features normalized

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ABCD Configuration & MC Closure



$X_{bb} > 0.5$ and $X_{Wqq} \leq 0.5|0.4$ (l|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A	0.71	0.27	0.53	0.02	—	—
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B	177.14	10.12	0.09	0.01	168	13.0
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	30.90	1.54	0.30	0.02	15	3.9
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	6617.60	132.59	0.10	0.01	6125	78.3

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{0.83 \pm 0.06}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{0.41 \pm 0.11}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{0.77}} \sqrt{\left(\frac{\mathbf{0.27}}{\mathbf{0.71}}\right)^2 + \left(\frac{\mathbf{0.06}}{\mathbf{0.83}}\right)^2} = 49.9\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 27.0\%$$

Final Result

Expected sig. 0.53 ± 0.02

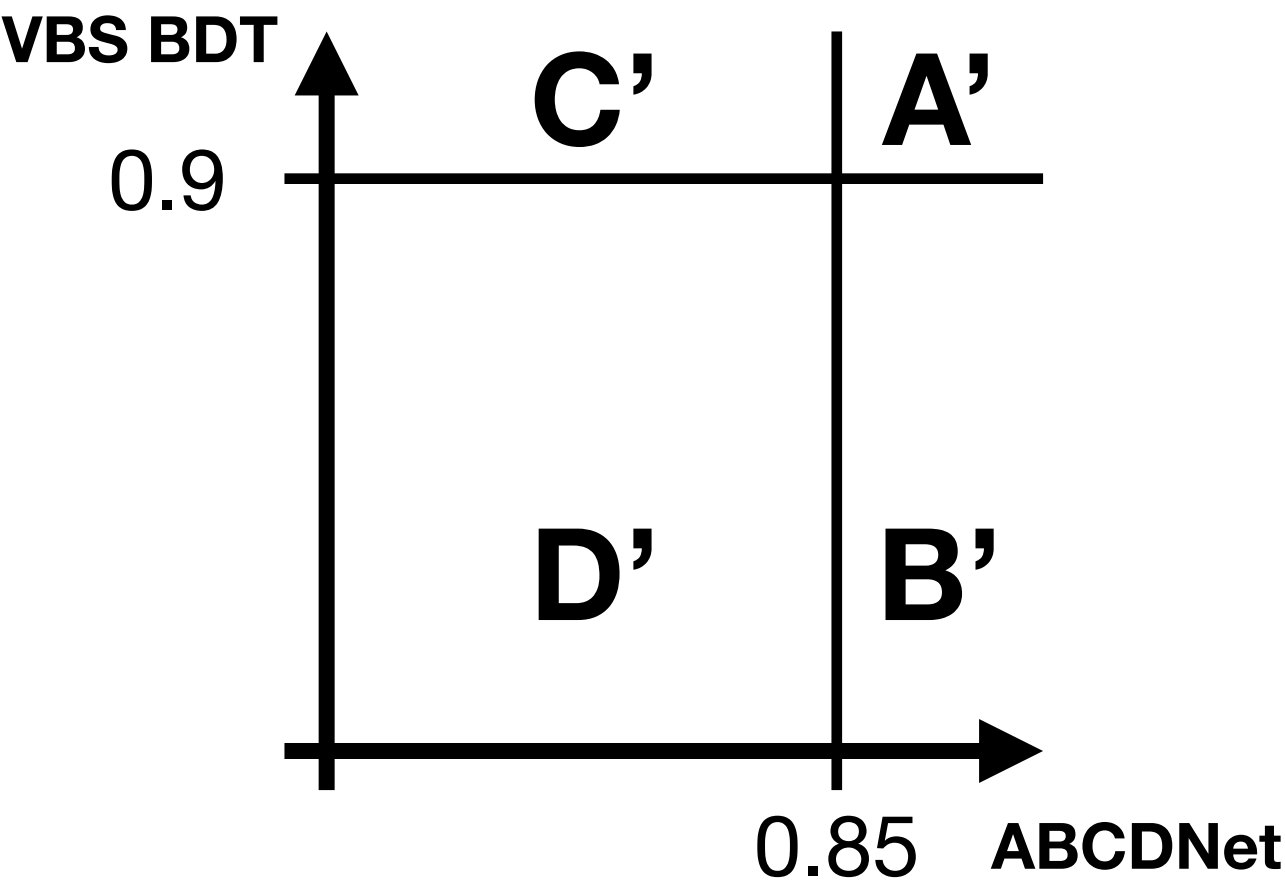
Predicted bkg. $0.41 \pm 0.11 \pm 0.21$

stat. *syst.*

Predicted significance ($S/\sqrt{B}$) is passable and the method closes in MC

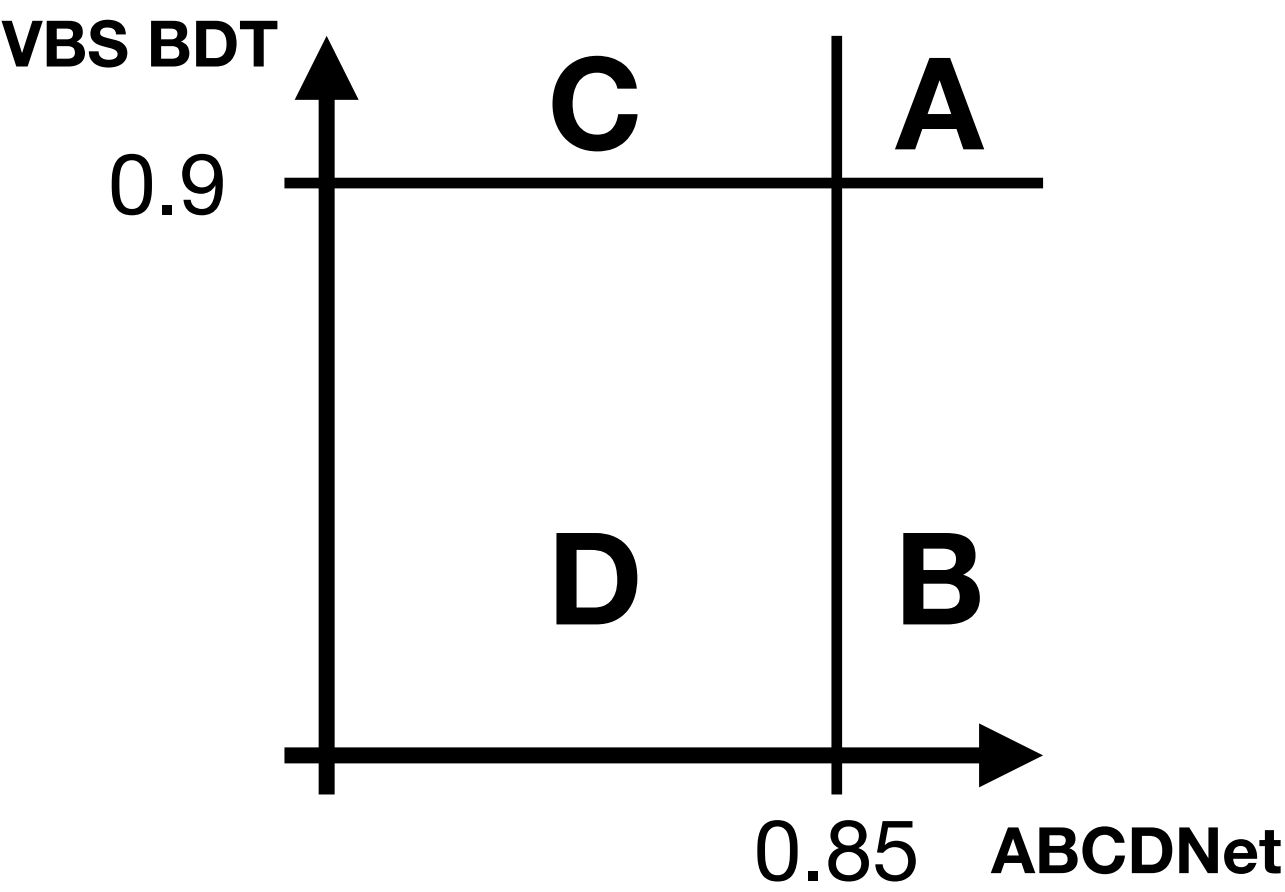


Closure in ParticleNet Sideband



$X_{bb} > 0.5$ and $X_{Wqq} \leq 0.5|0.4$ (ld|tr)

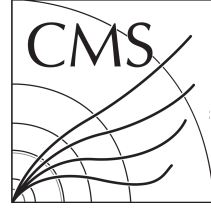
Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
$VBS\ BDT > 0.9$ and $ABCDNet > 0.9$	A'	0.71	0.27	0.53	0.02	—	—
$VBS\ BDT \leq 0.9$ and $ABCDNet > 0.9$	B'	177.14	10.12	0.09	0.01	168	13.0
$VBS\ BDT > 0.9$ and $ABCDNet \leq 0.9$	C'	30.90	1.54	0.30	0.02	15	3.9
$VBS\ BDT \leq 0.9$ and $ABCDNet \leq 0.9$	D'	6617.60	132.59	0.10	0.01	6125	78.3



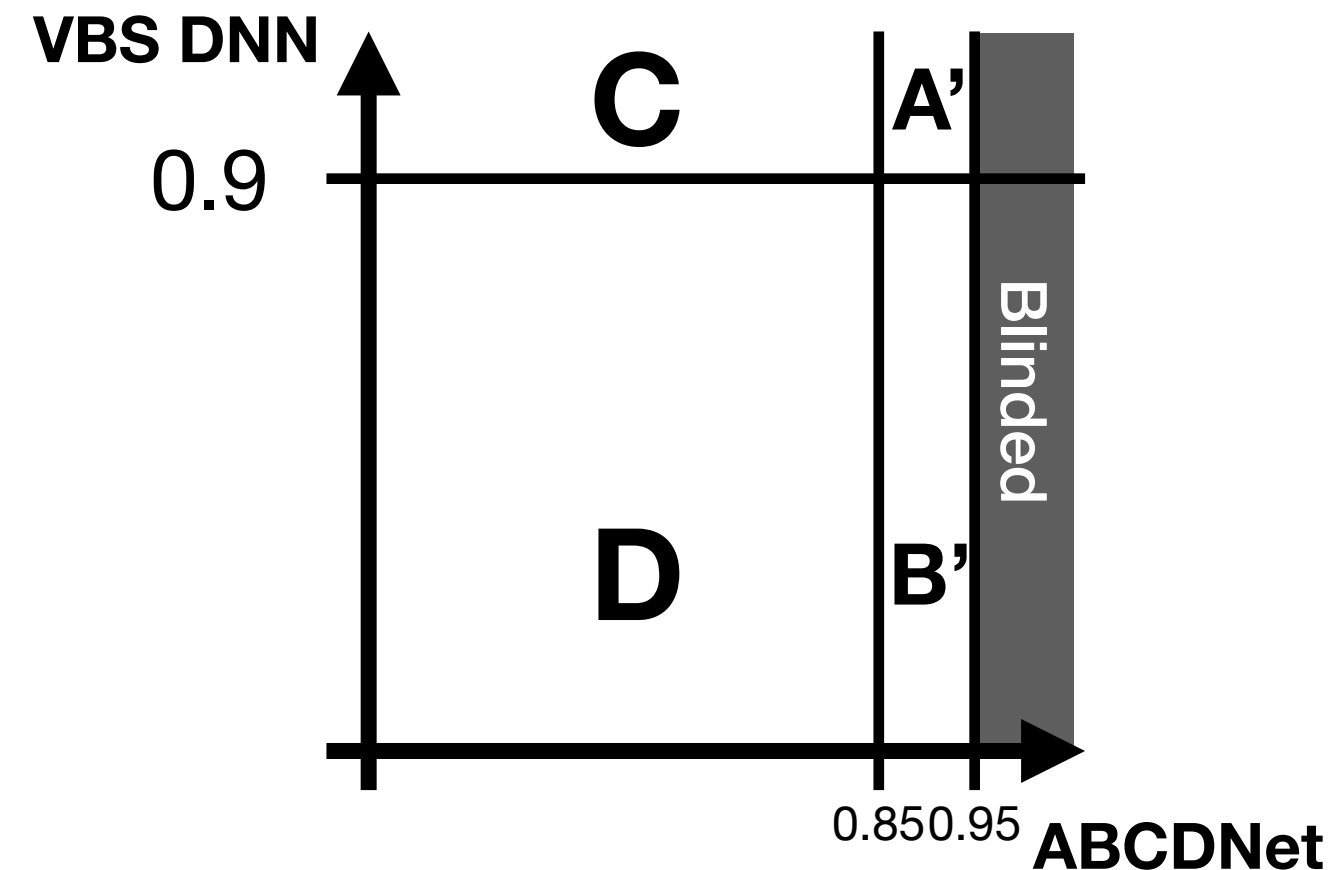
$X_{bb} > 0.5$ and $X_{Wqq} > 0.5|0.4$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
$VBS\ BDT > 0.9$ and $ABCDNet > 0.9$	A	0.95	0.37	6.88	0.07	—	—
$VBS\ BDT \leq 0.9$ and $ABCDNet > 0.9$	B	189.89	8.37	0.92	0.03	185	13.6
$VBS\ BDT > 0.9$ and $ABCDNet \leq 0.9$	C	56.11	2.29	2.35	0.04	33	5.7
$VBS\ BDT \leq 0.9$ and $ABCDNet \leq 0.9$	D	7271.69	125.39	0.54	0.02	7817	88.4

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
$VBS\ BDT > 0.9$ and $ABCDNet > 0.9$	A'/A	0.74	0.40	12.97	0.51	—	—
$VBS\ BDT \leq 0.9$ and $ABCDNet > 0.9$	B'/B	0.93	0.07	10.01	0.96	0.9	0.10
$VBS\ BDT > 0.9$ and $ABCDNet \leq 0.9$	C'/C	0.55	0.04	7.71	0.41	0.5	0.14
$VBS\ BDT \leq 0.9$ and $ABCDNet \leq 0.9$	D'/D	0.91	0.02	5.59	0.55	0.8	0.01



ABCD Configuration & MC Closure



$X_{bb} > 0.5$ and $X_{Wqq} \leq 0.5|0.4$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS BDT > 0.9 and ABCDNet > 0.9	A'	0.43	0.16	0.18	0.01	1	1.0
VBS BDT ≤ 0.9 and ABCDNet > 0.9	B'	125.47	9.36	0.04	0.01	133	11.53
VBS BDT > 0.9 and ABCDNet ≤ 0.9	C	30.90	1.54	0.30	0.02	15	3.87
VBS BDT ≤ 0.9 and ABCDNet ≤ 0.9	D	6617.60	132.59	0.10	0.01	6125	78.26

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{0.59 \pm 0.05}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{0.33 \pm 0.09}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{0.51}} \sqrt{\left(\frac{\mathbf{0.16}}{\mathbf{0.43}}\right)^2 + \left(\frac{\mathbf{0.05}}{\mathbf{0.59}}\right)^2} = 73.8\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 27.3\%$$

Final Result

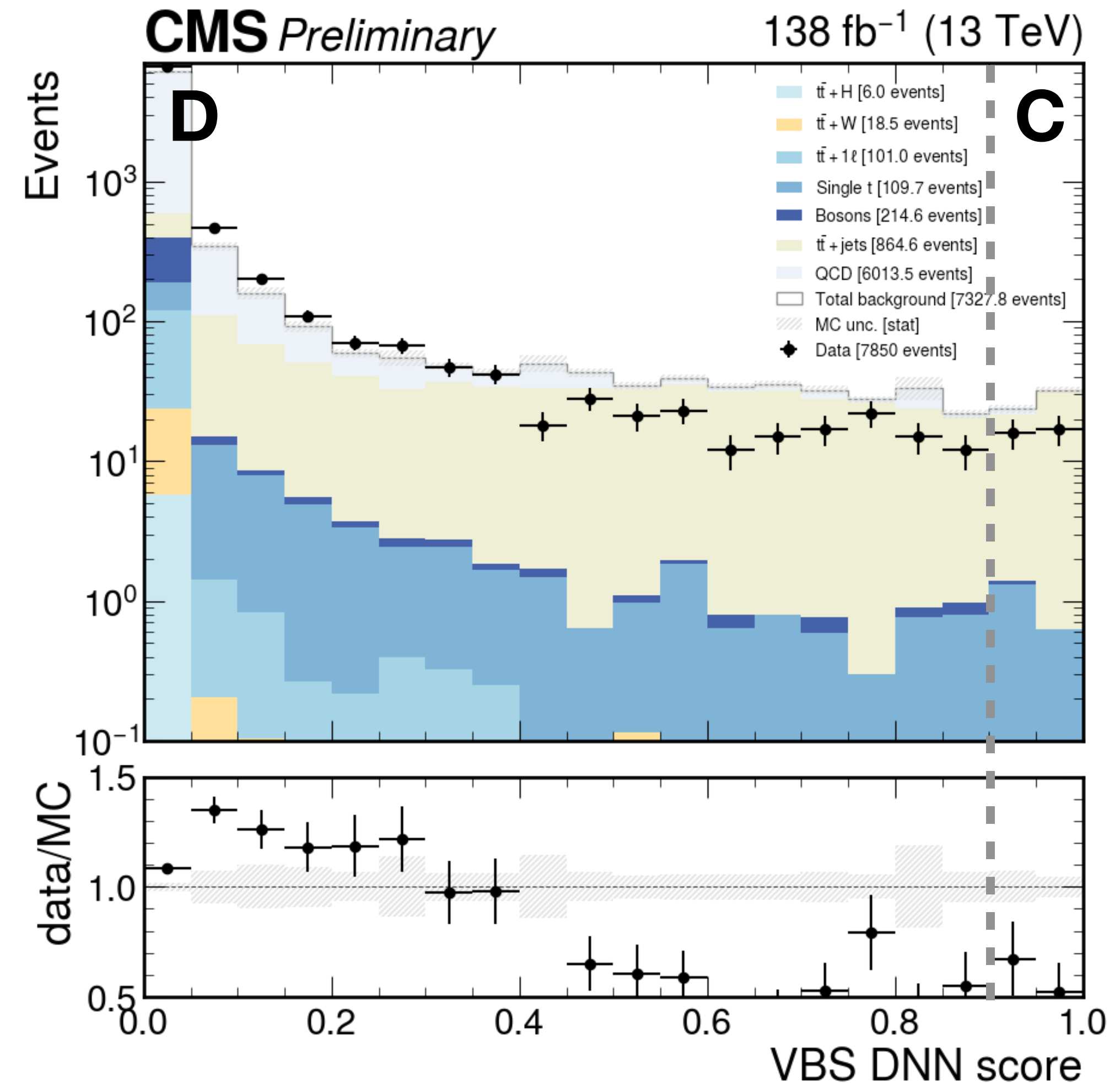
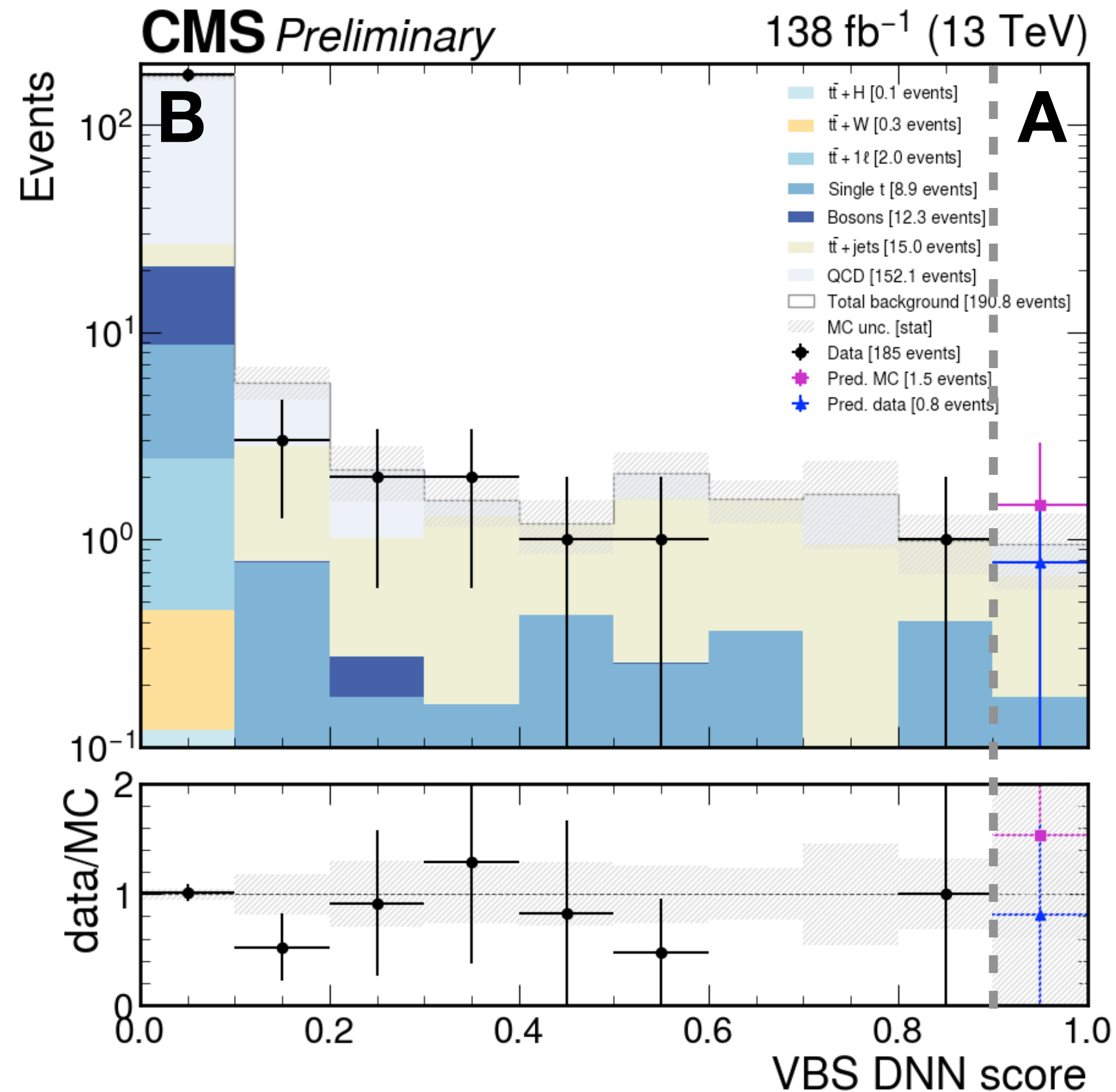
Expected sig. 0.18 ± 0.01

Predicted bkg. $0.33 \pm 0.09 \pm 0.24$

stat. syst.

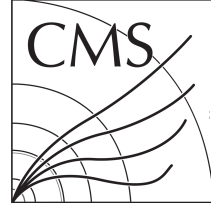
Predicted significance ($S/\sqrt{B}$) is passable and the method closes in MC

Reweighted vs. Single-point

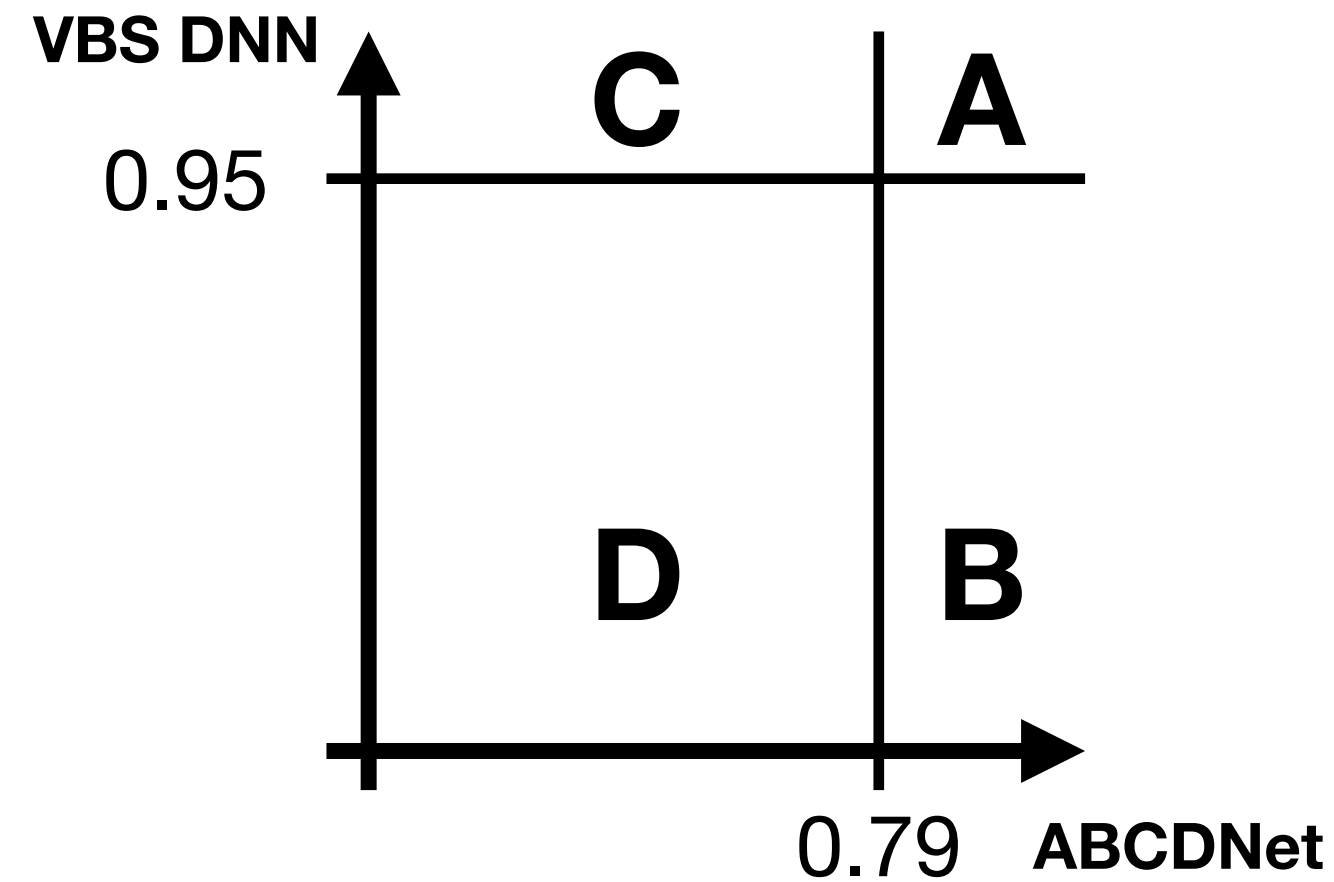


Seems to be a systematic issue in data/MC going from D to C

Backup



ABCD Configuration & MC Closure



$X_{bb} > 0.5$ and $X_{Wqq} > 0.3|0.3$ (ld|tr)

Selection	Region	Bkg	Bkg err	Sig	Sig err	Data	Data err
VBS DNN > 0.9 and ABCDNet > 0.9	A	1.00	0.28	7.23	0.08	—	—
VBS DNN ≤ 0.9 and ABCDNet > 0.9	B	532.17	15.82	1.86	0.04	510	22.58
VBS DNN > 0.9 and ABCDNet ≤ 0.9	C	52.21	1.96	1.83	0.04	23	4.80
VBS DNN ≤ 0.9 and ABCDNet ≤ 0.9	D	13759.61	182.28	0.79	0.02	13811	117.52

$$A_{MC} = B_{MC} \times C_{MC} / D_{MC} = \mathbf{2.02 \pm 0.10}$$

$$A_{pred} = B_{data} \times C_{data} / D_{data} = \mathbf{0.85 \pm 0.18}$$

Error propagation:

$$\epsilon_{syst} = \frac{1}{\mathbf{1.51}} \sqrt{\left(\frac{\mathbf{0.28}}{\mathbf{1.00}}\right)^2 + \left(\frac{\mathbf{0.10}}{\mathbf{2.02}}\right)^2} = 19.0\%$$

$$\epsilon_{stat} = \sqrt{\frac{1}{B_{data}} + \frac{1}{C_{data}} + \frac{1}{D_{data}}} = 21.3\%$$

Final Result

Expected sig. 7.23 ± 0.08

Predicted bkg. $0.85 \pm 0.18 \pm 0.16$

stat. *syst.*

Predicted significance ($S/\sqrt{B}$) is very good and the method roughly closes in MC